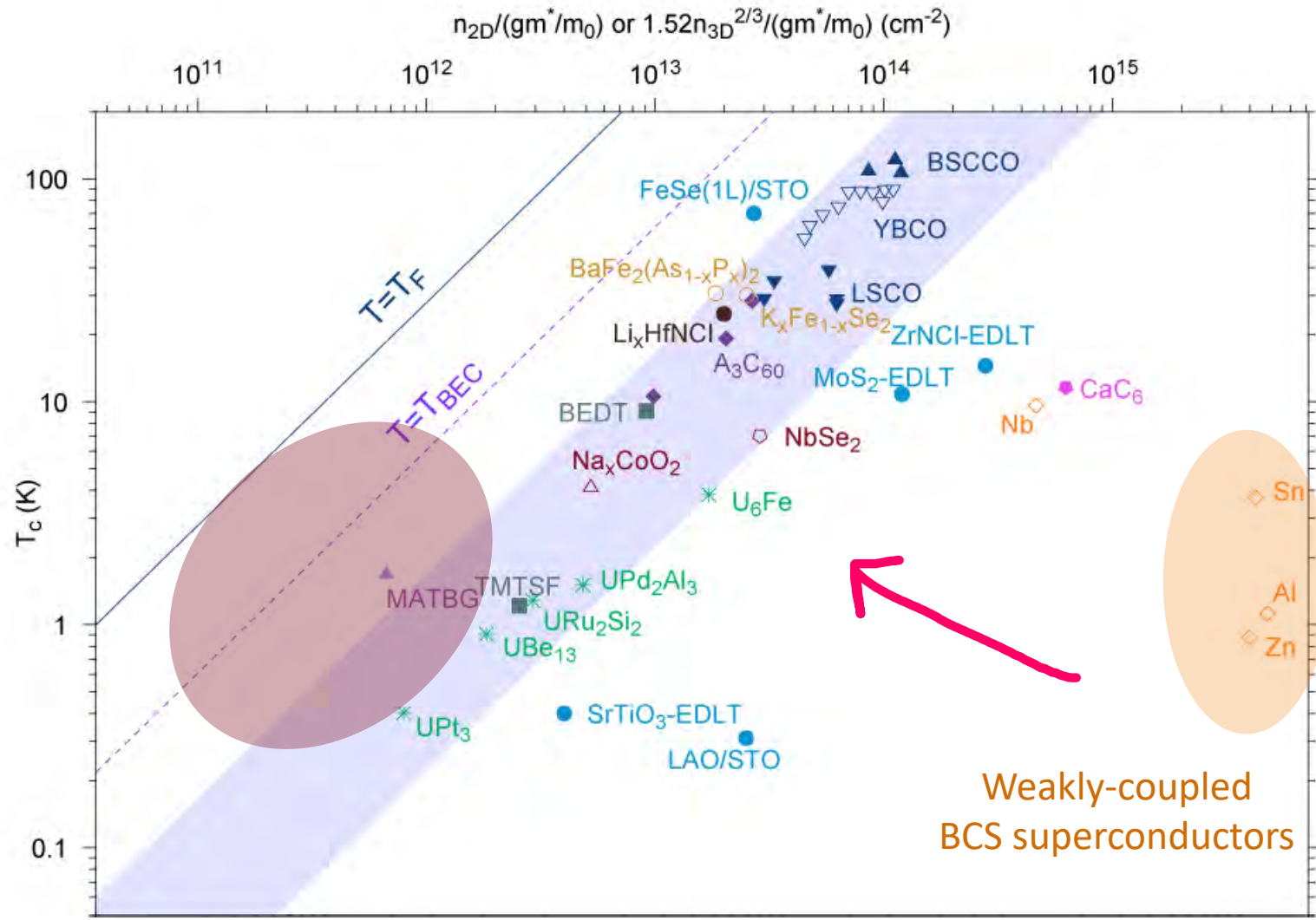


The Magic Family

of Twisted Graphene Superconductors

Jeong Min (Jane) Park
2024 Theory Winter School

Unexplored regime of superconductivity



Strongly-coupled superconductors

Weakly-coupled
BCS superconductors

- 2-dimensional twisted materials for correlated physics
 - Magic-angle twisted bilayer graphene
- Magic-angle twisted trilayer graphene
- The magic family
- Outlook

How to study strongly correlated physics?

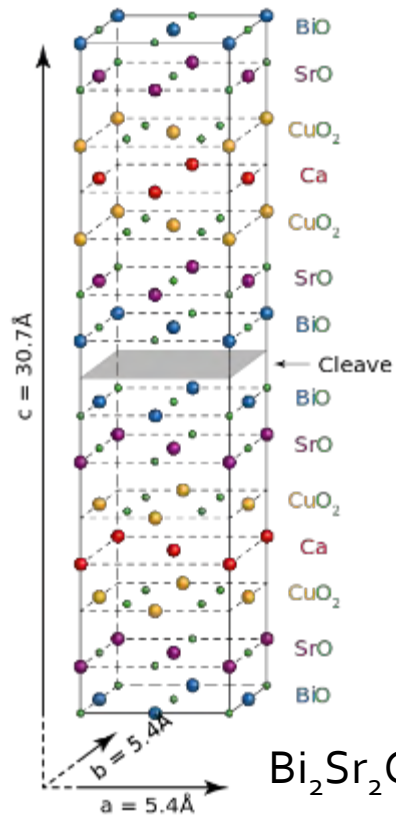


Quantum Materials

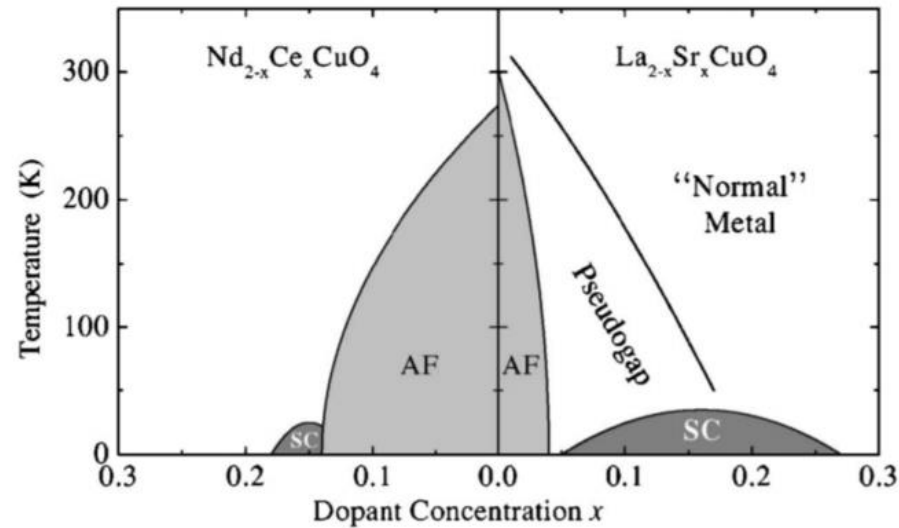
Lattice scale ~ **few Å**

Temperature scale

~ **100-1,000 Kelvin**



“Doping”



← *electron* -doping

→ *hole* -doping

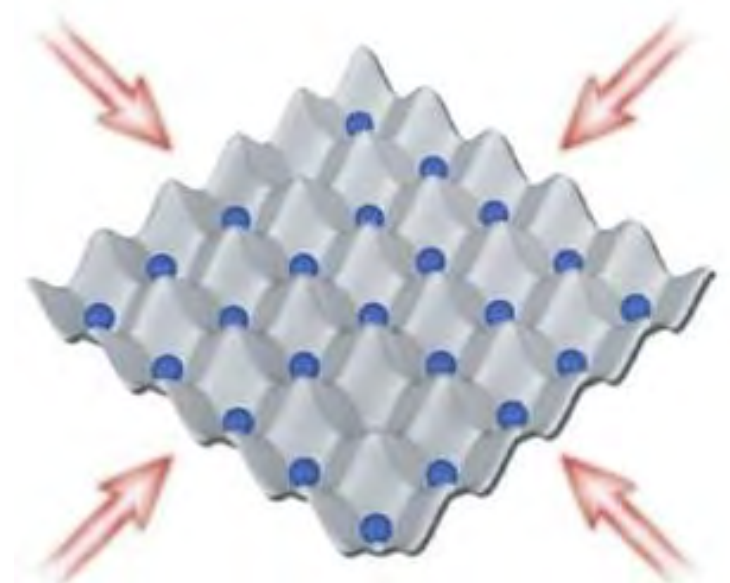
Damascelli, Hussain & Shen, *Rev. Mod. Phys.* (2003)

Cold Atoms Optical Lattices

Length scale ~ **1 micron**

Temperature scale

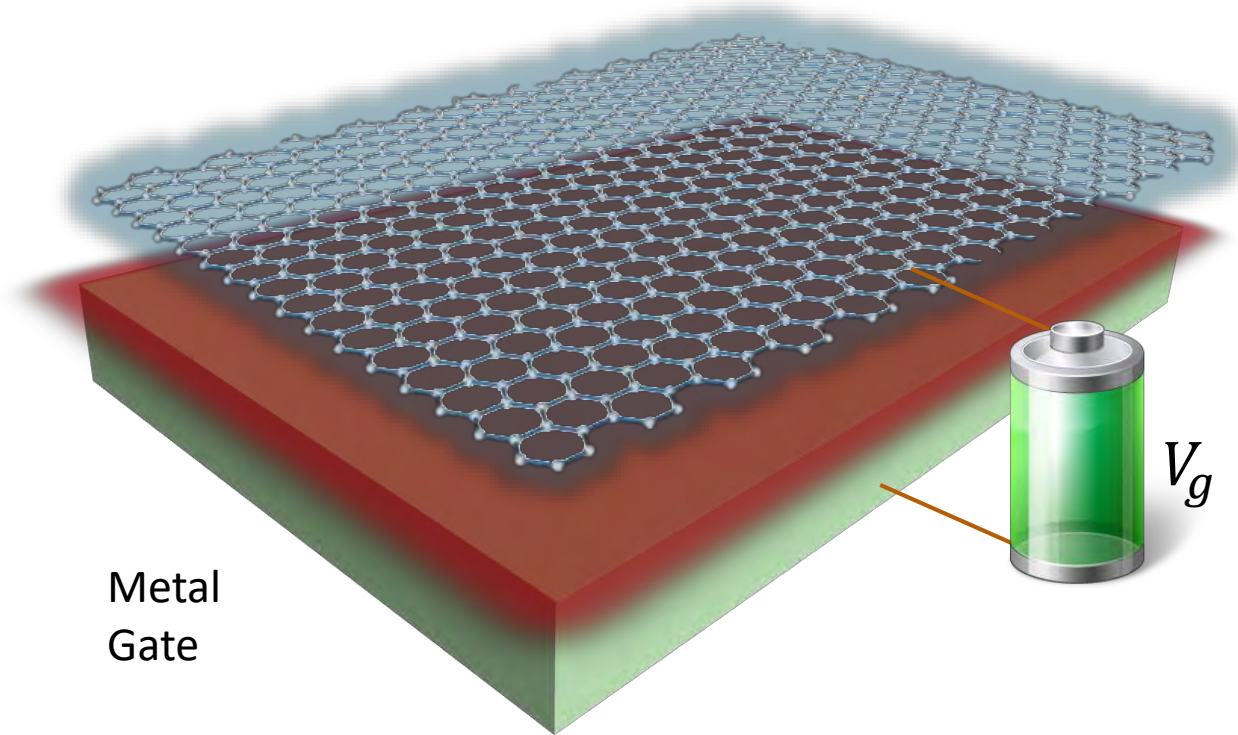
~ **0.1-1 nanoKelvin**



Doping tunability of 2D materials

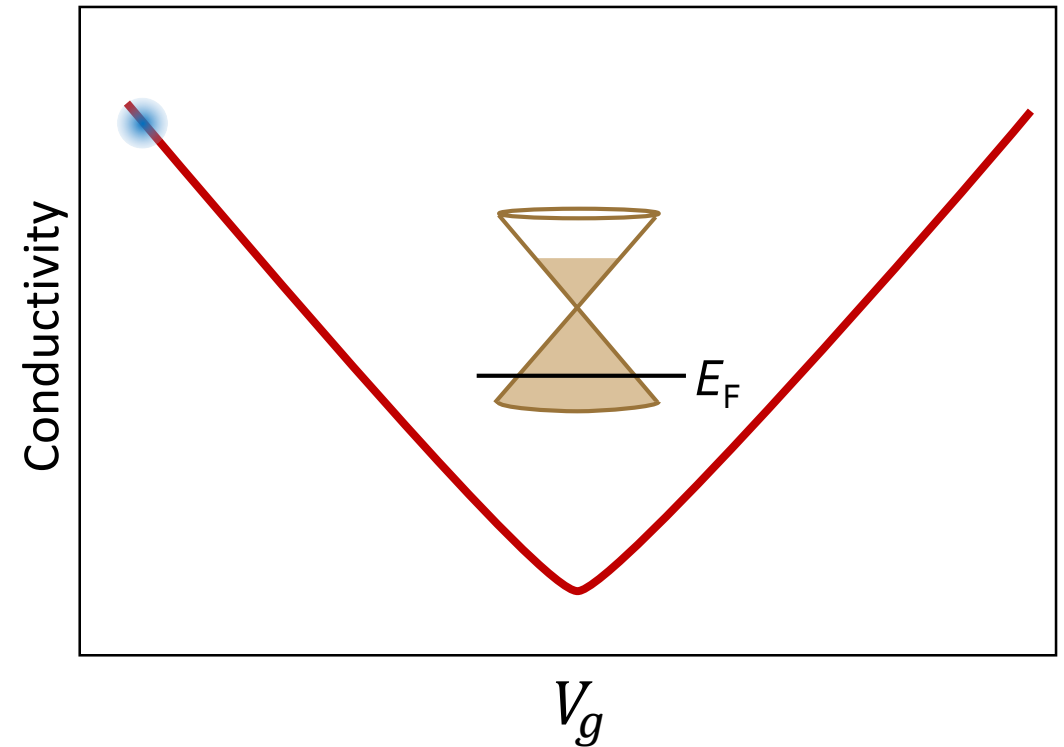


Graphene

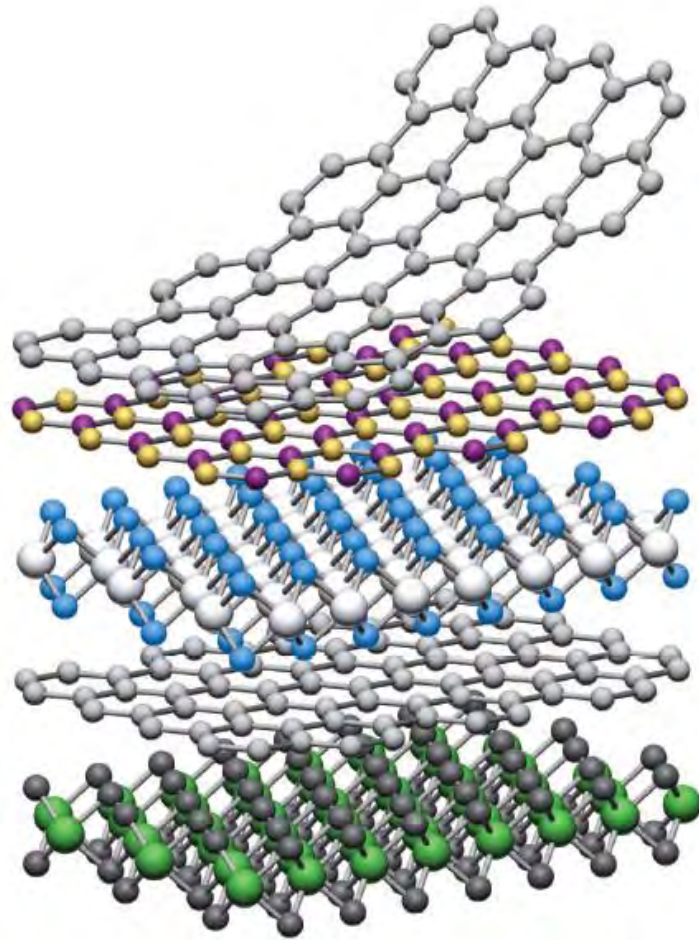


Metal
Gate

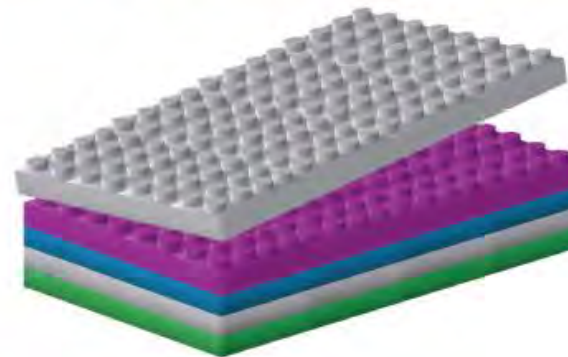
$$\text{Charge density } n = CV_g/e$$



Stacking tunability of 2D materials

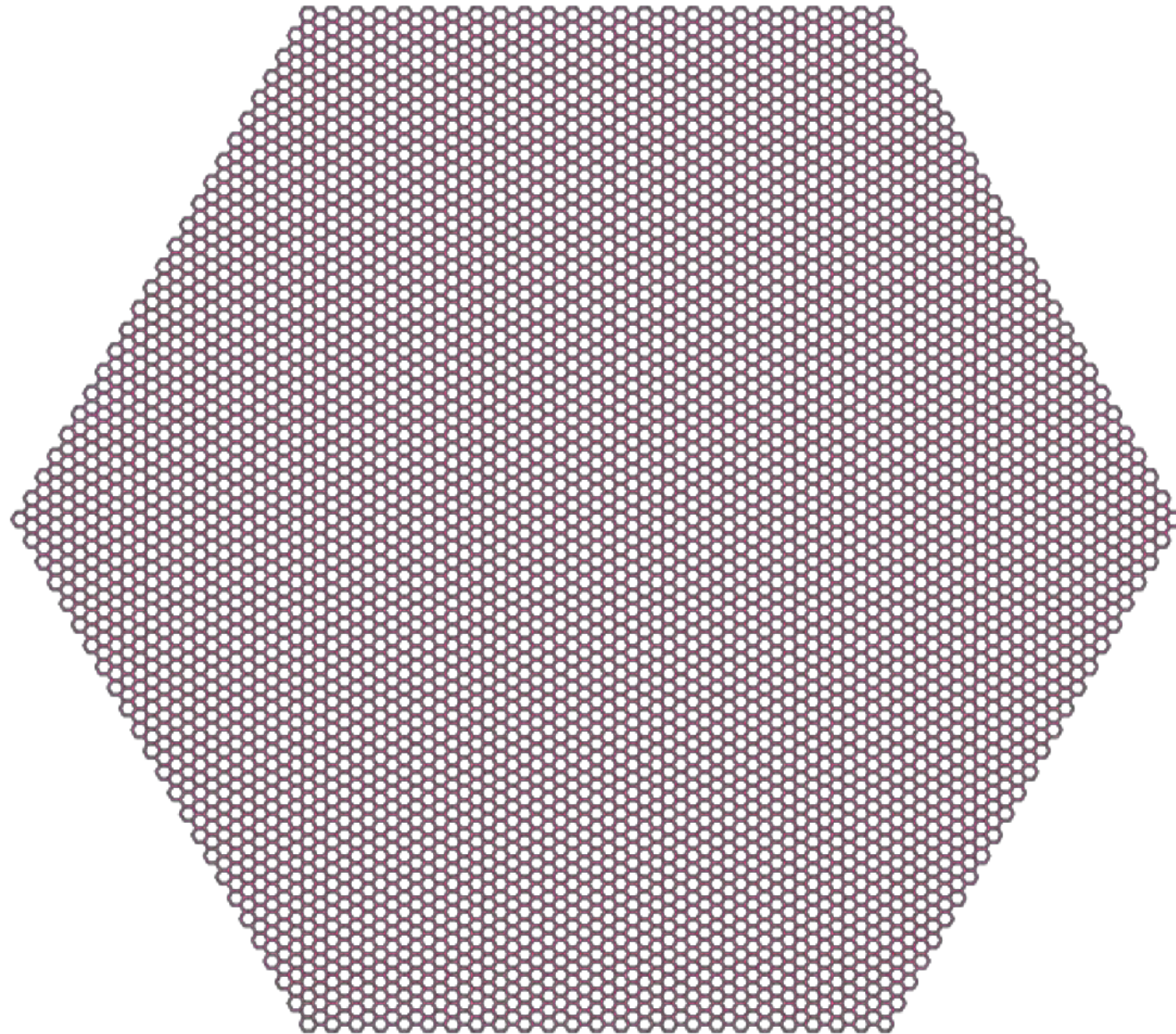


	Graphene	
	hBN	
	MoS ₂	
	WSe ₂	
	Fluorographene	

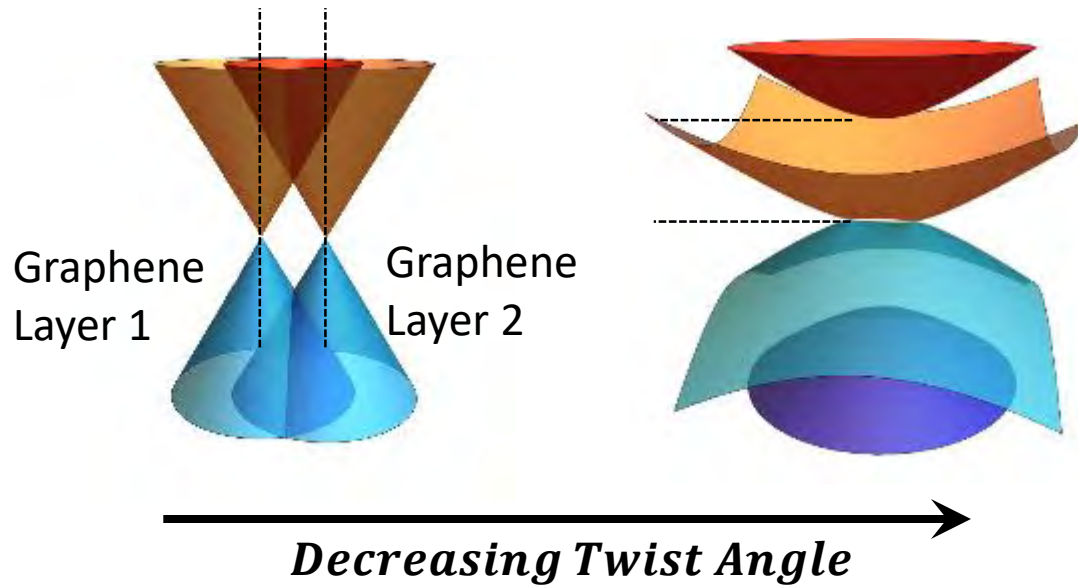


Geim & Grigorieva, Nature (2013)

Even more: twist angle!

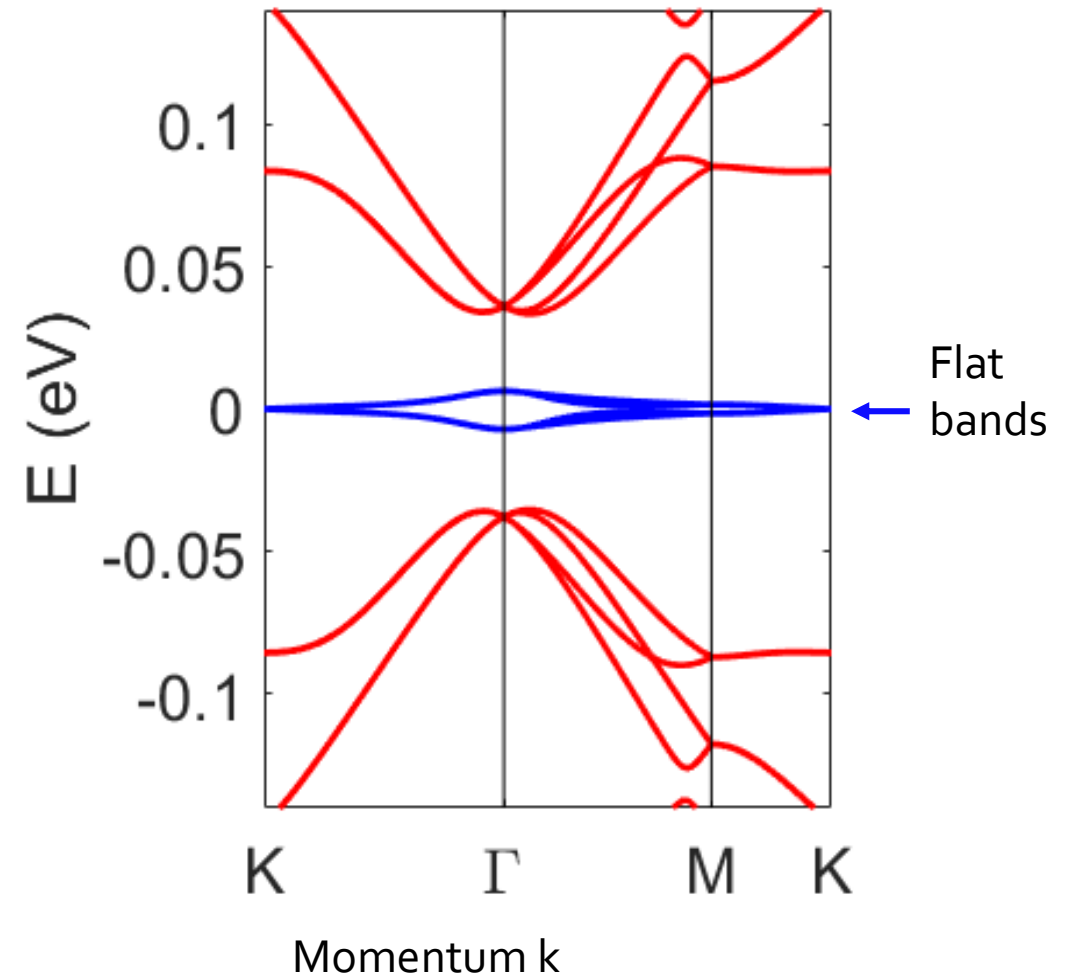


Designing flat bands

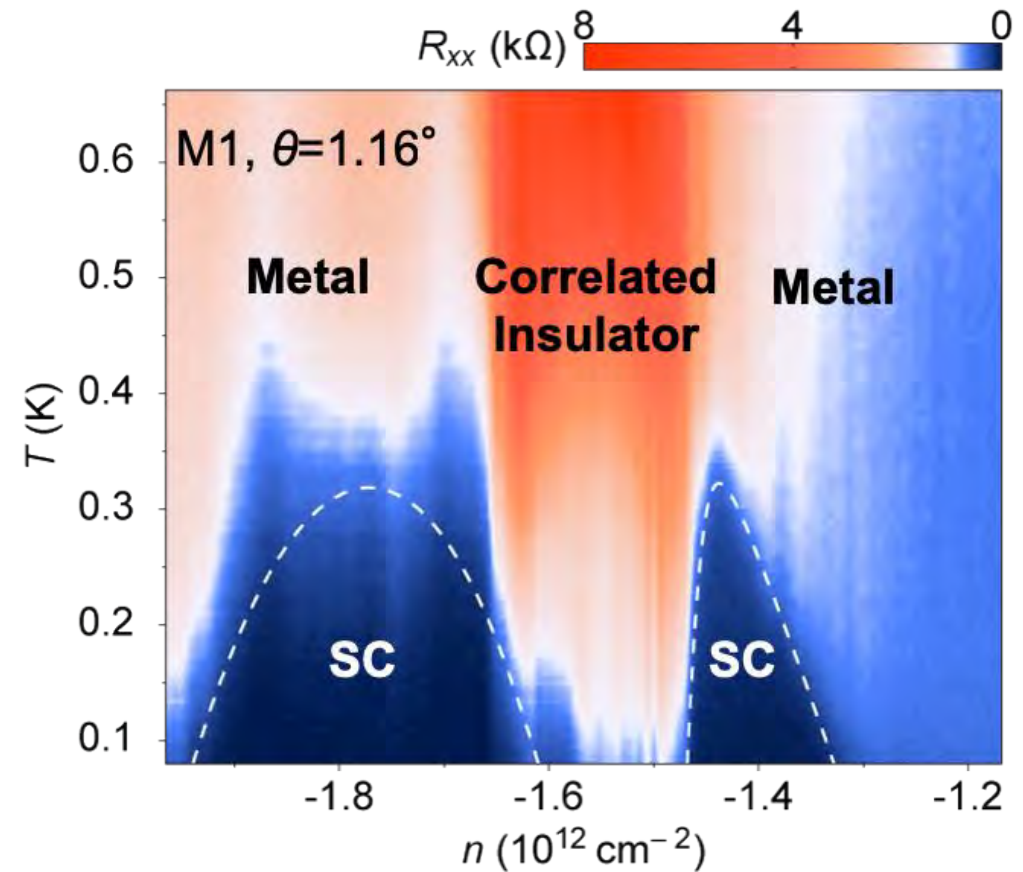
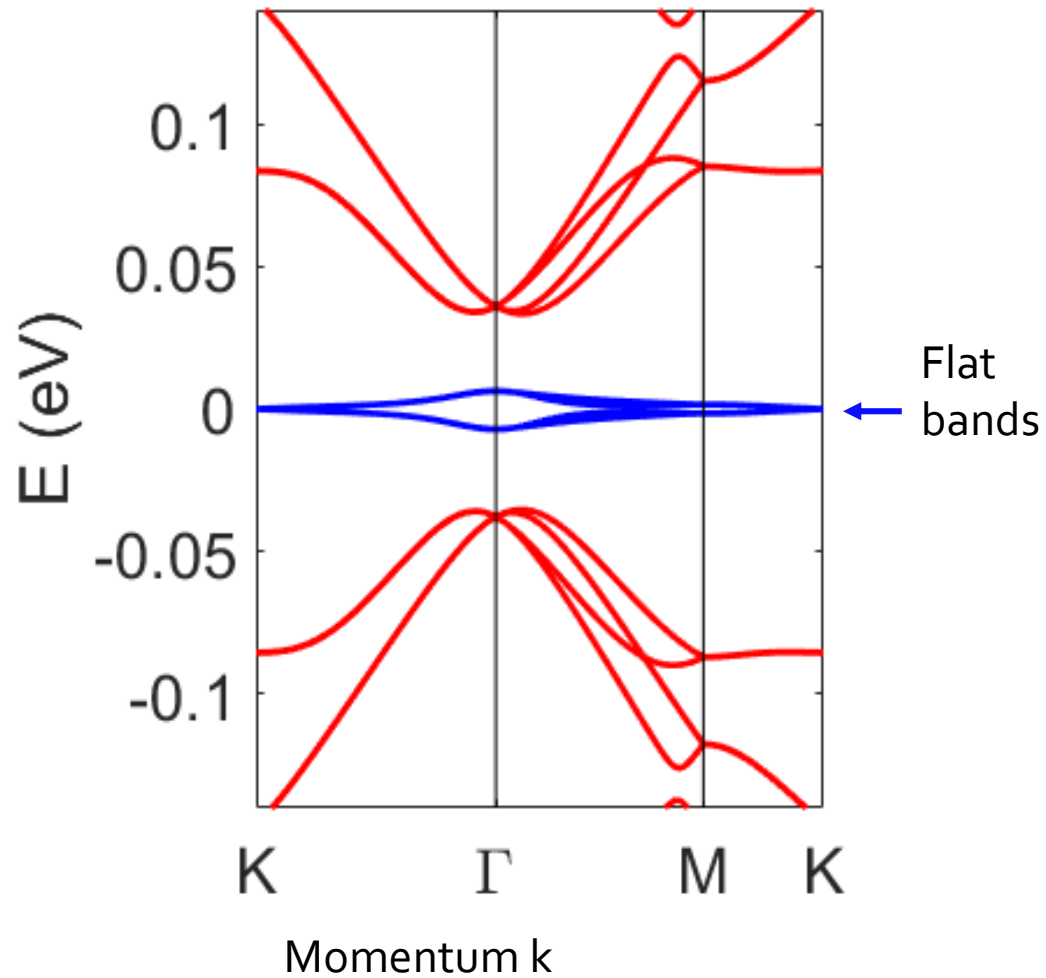


“Flat Band” condition is reached
at the “Magic Angle”

$$\theta_{M1} \approx 1.1^\circ$$

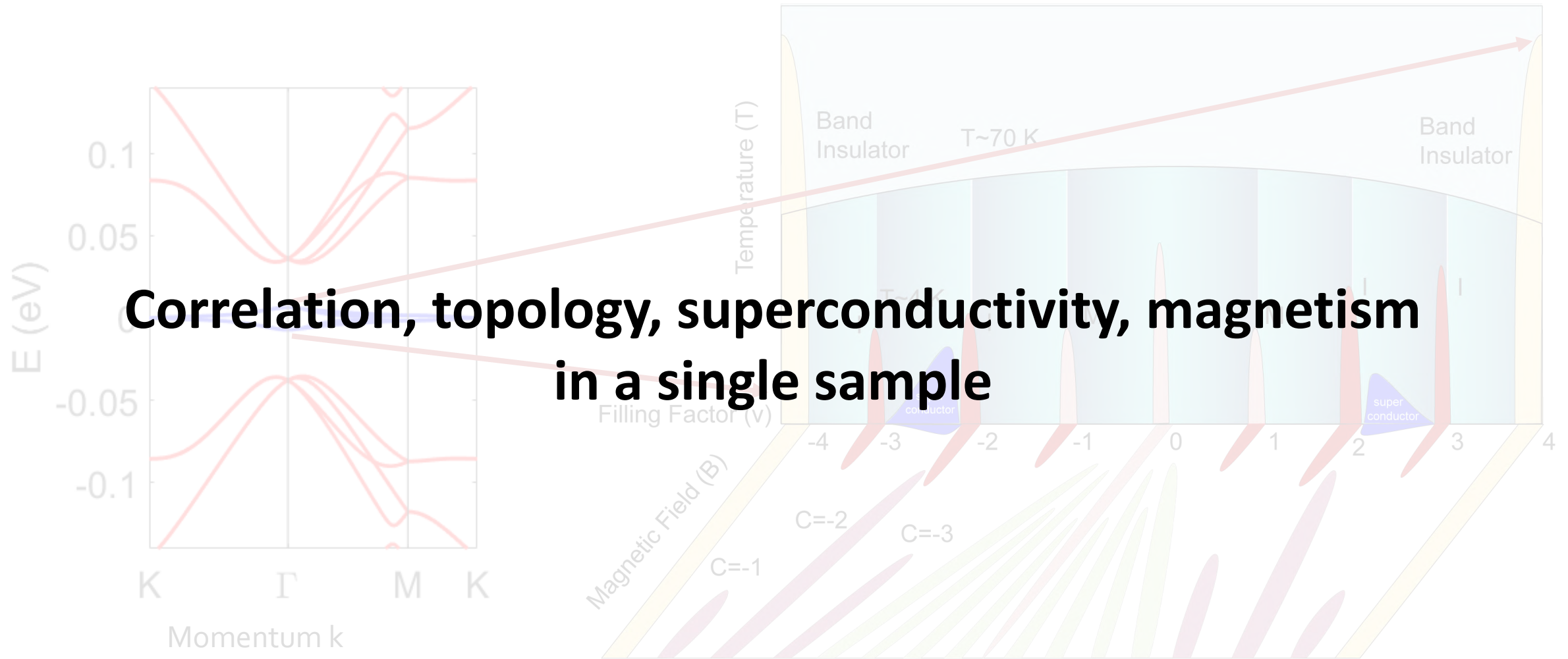


Superconductivity in the flat bands



Low-density superconductor

So many phases in a single material

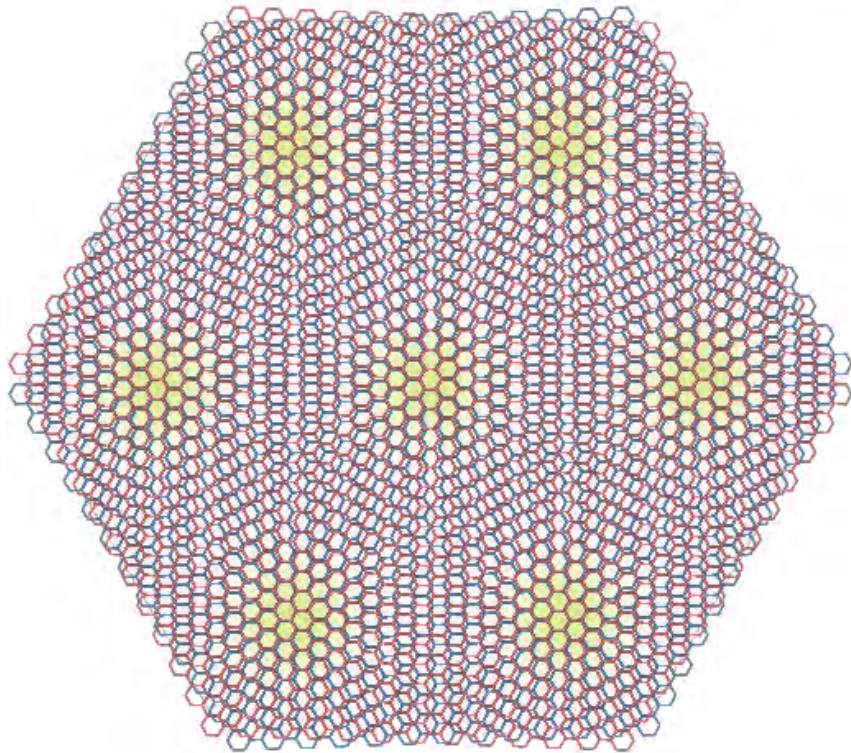


Moiré is different



Moiré Quantum Matter

Moiré length ~ **10nm**



Correlated Insulators
(MATBG, ABC/hBN, Twisted Bi-Bi, TMD moiré heterostructures, etc)

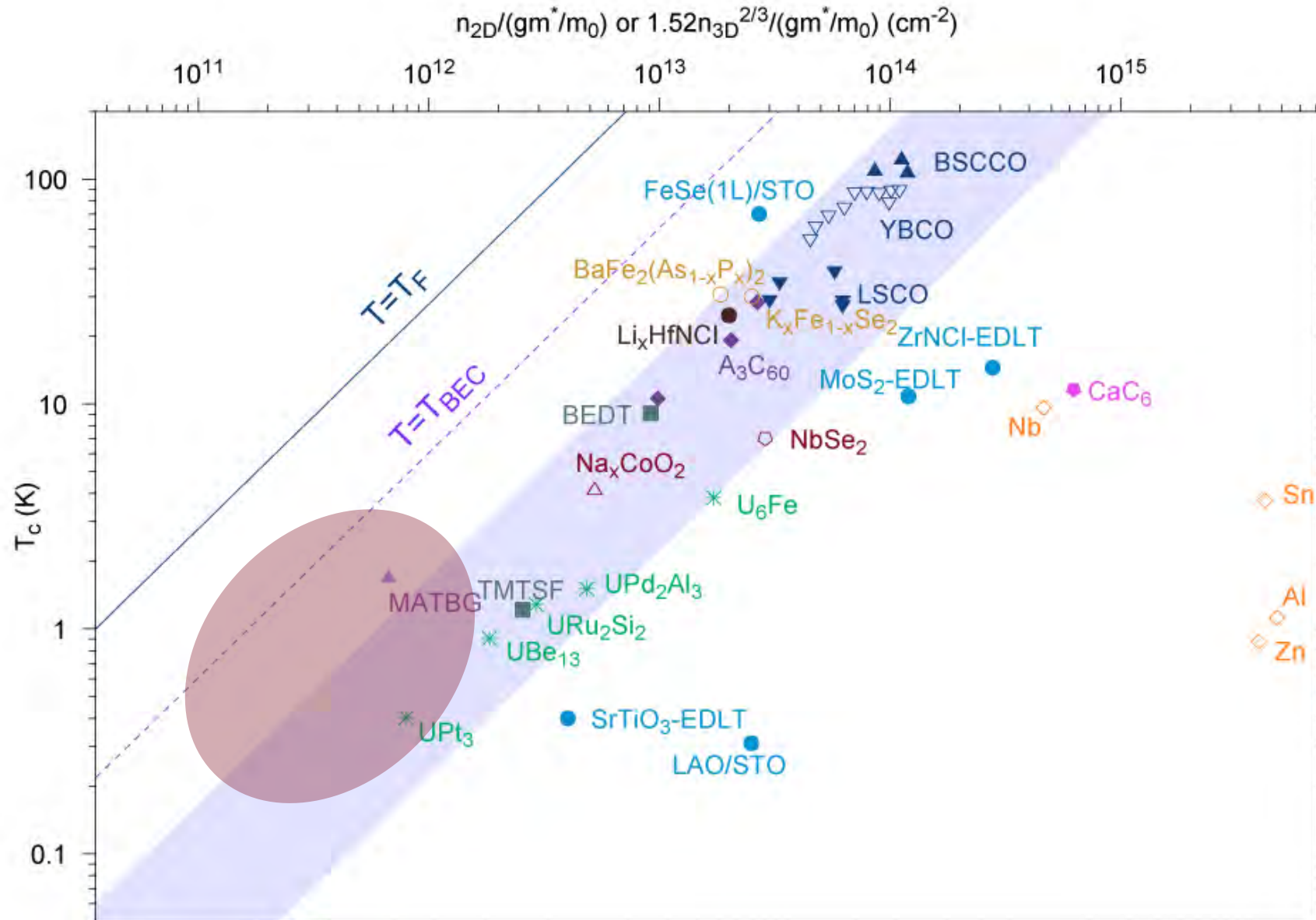
Robust Superconductivity
(MATBG, signatures in other systems)

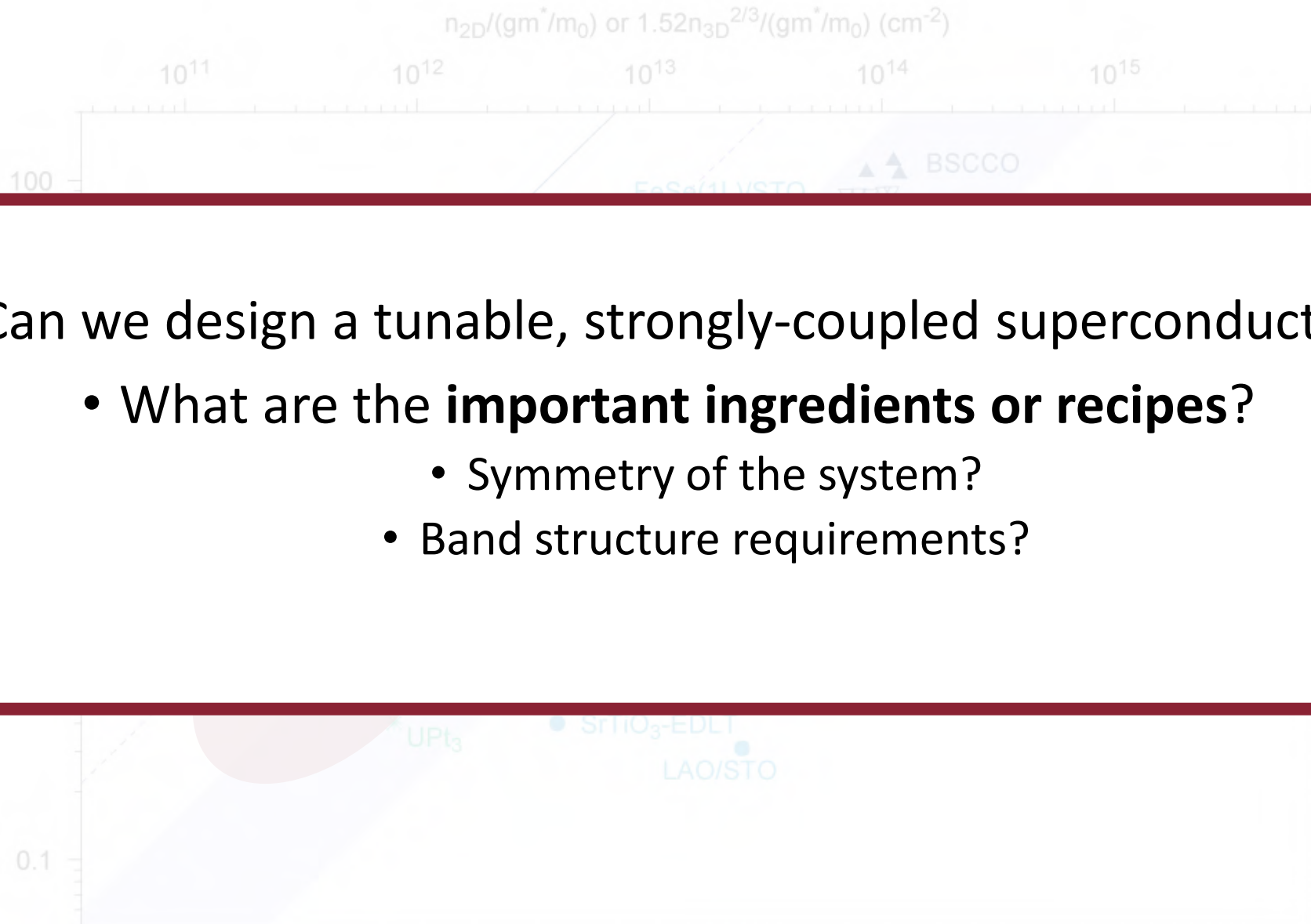
Topological Phases
(MATBG, MATBG/hBN, ABC/hBN, Twisted Bi-Bi, Twisted Mono-Bi, etc))

Magnetism
(MATBG/hBN, ABC/hBN, Twisted Mono-Bi)

Moiré Ferroelectricity
(Twisted BN/BN, BLG/BN, Twisted TMD/TMD)

Moiré is different for superconductivity?

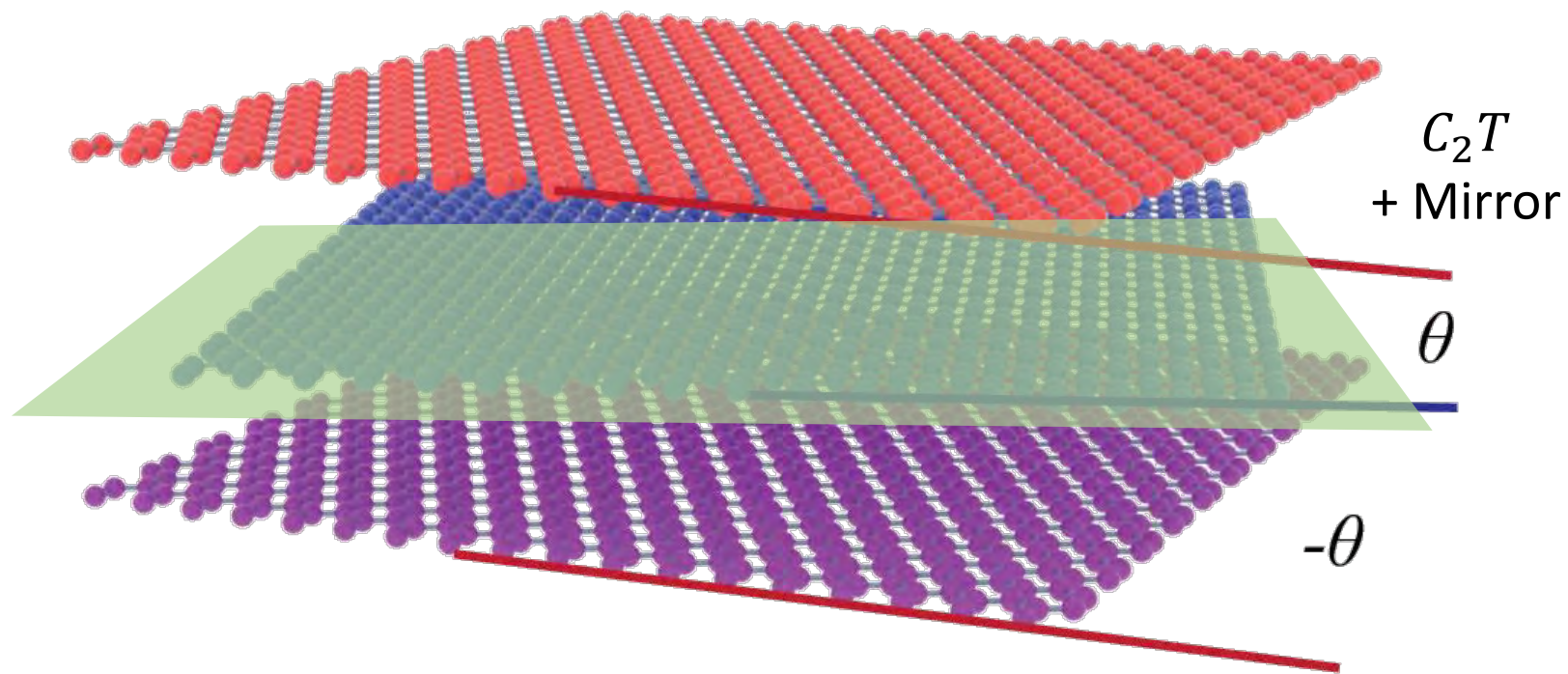




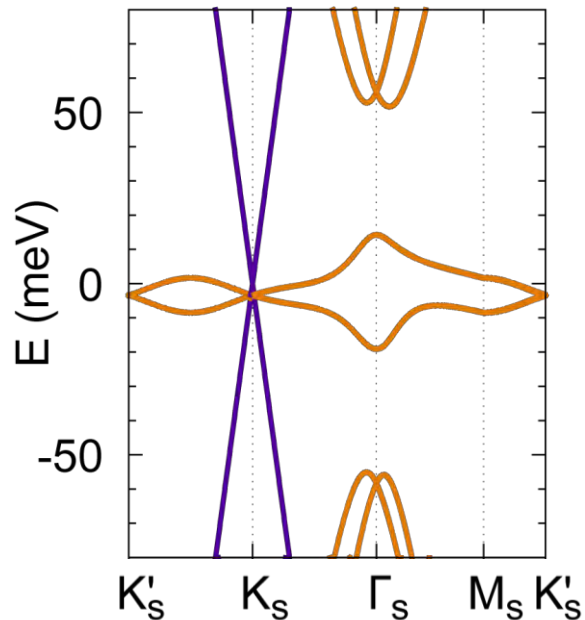
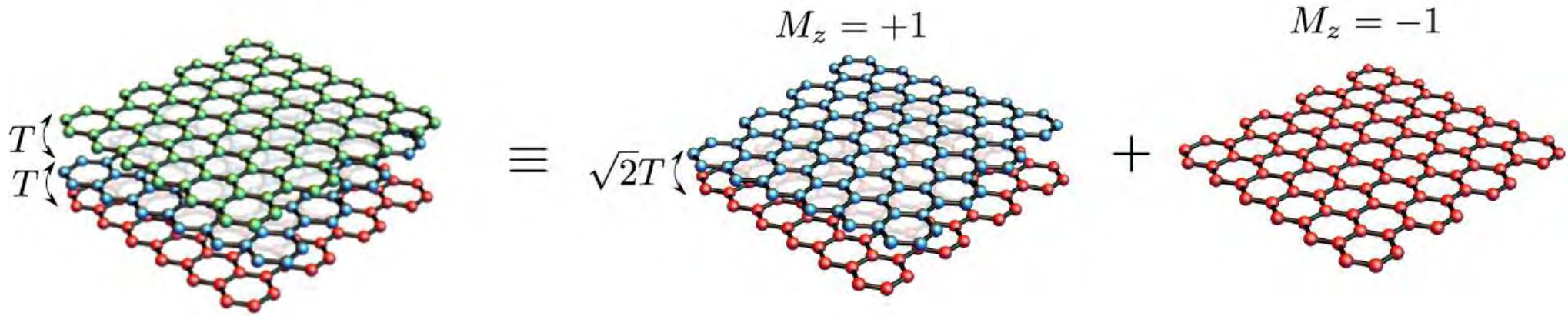
- Can we design a tunable, strongly-coupled superconductor?
 - What are the **important ingredients or recipes**?
 - Symmetry of the system?
 - Band structure requirements?

- 2-dimensional materials for strongly correlated physics
 - Magic-angle twisted bilayer graphene
- **Magic-angle twisted trilayer graphene**
- The magic family
- Outlook

Magic-angle twisted trilayer graphene (MATTG)



Magic-angle twisted trilayer graphene (MATTG)



$C_2T \rightarrow$ protects the Dirac points
 Mirror \rightarrow protects the separate Dirac band

$$H = \begin{pmatrix} \text{MATTG} & & \\ & 0 & \\ & & 0 \\ & & & \text{MLG} \end{pmatrix}$$

$$\theta_{\text{MATTG}} = \theta_{\text{MATBG}} \times \sqrt{2} \approx 1.1^\circ \times \sqrt{2} \approx 1.56^\circ$$

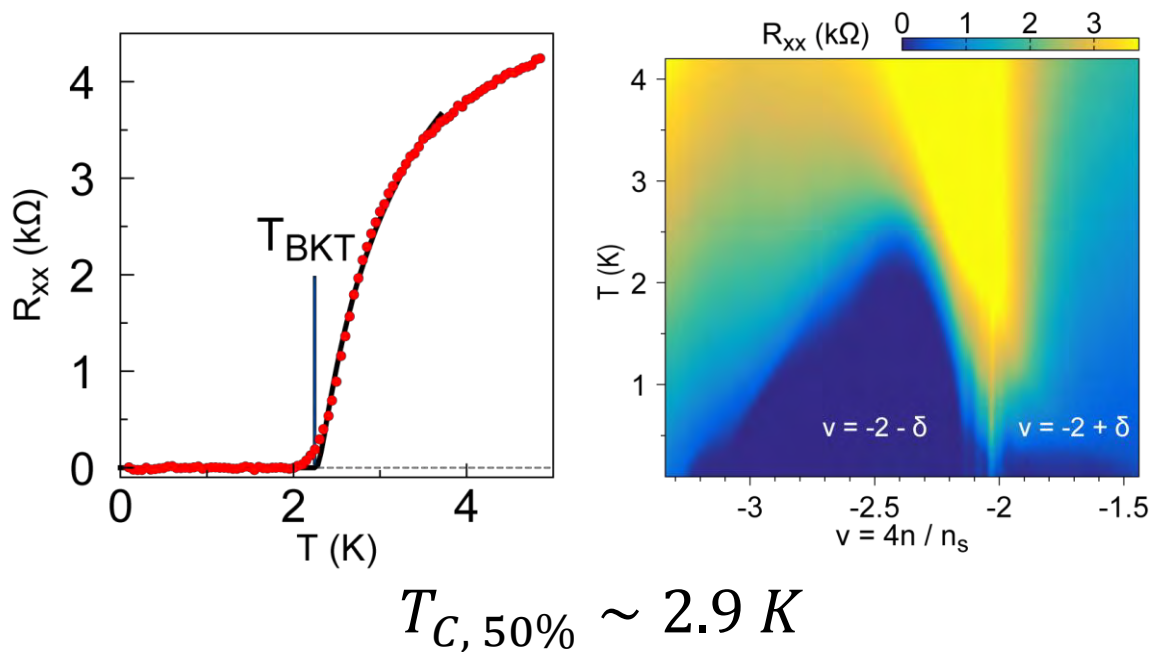
Khalaf, Vishwanath et al. *Phys. Rev. B* **100**, 085109 (2019)

JMP et al. *Nature* **590**, 249 (2021)

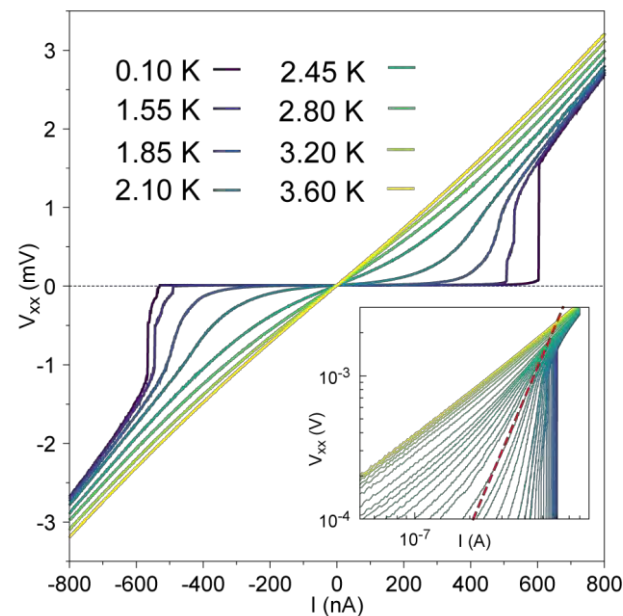
MATTG is a robust superconductor



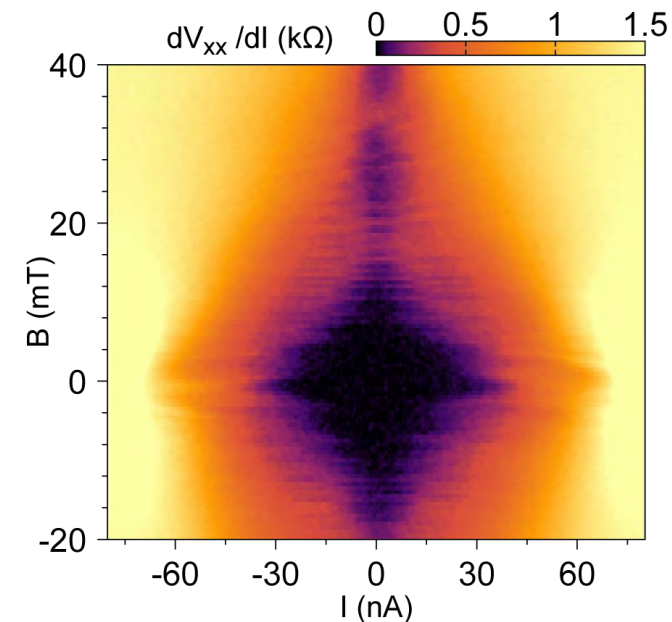
1. Zero resistance



2. Sharp Switching V-I characteristics

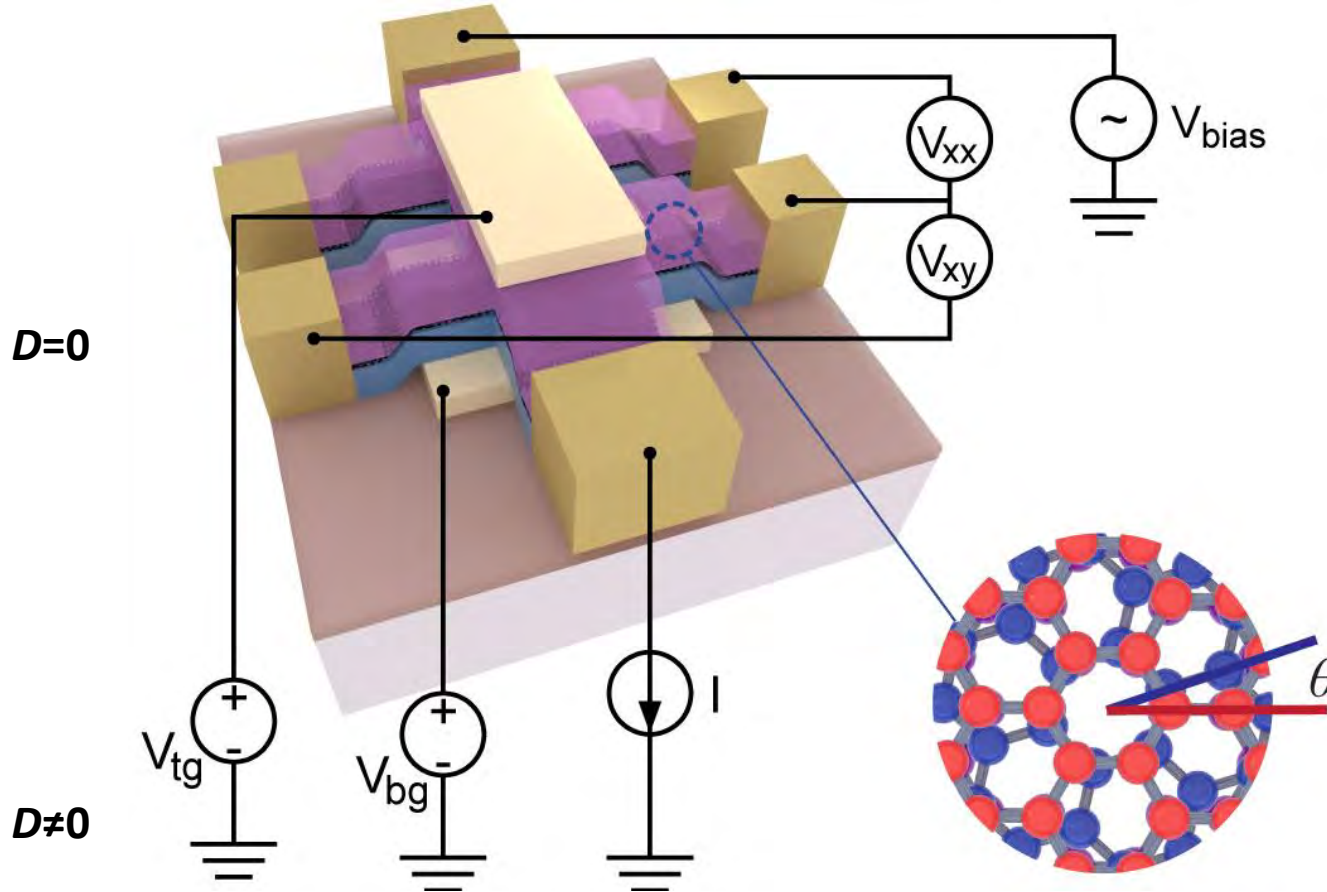
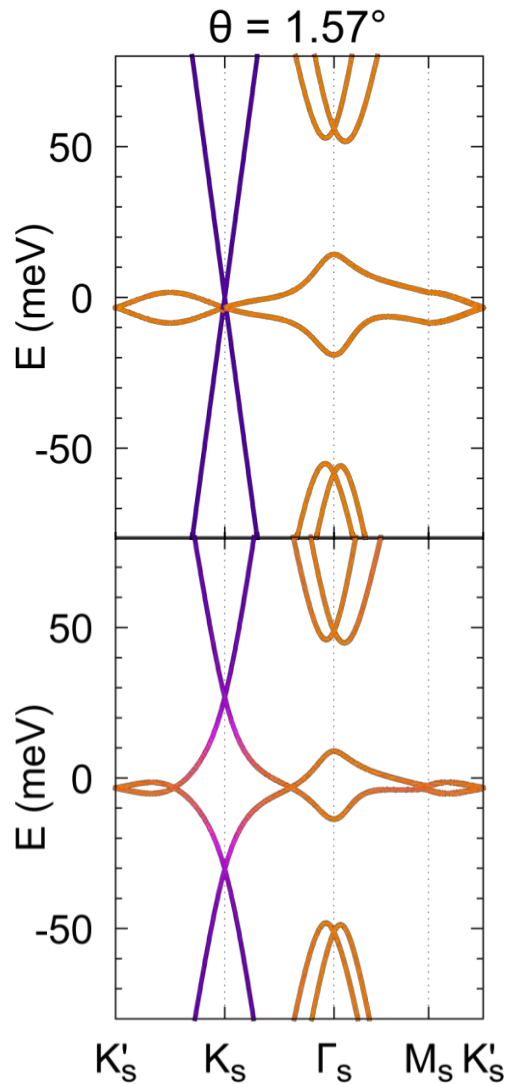


3. Josephson phase coherence



MATTG is a robust moiré superconductor!

Further tunability: band structure

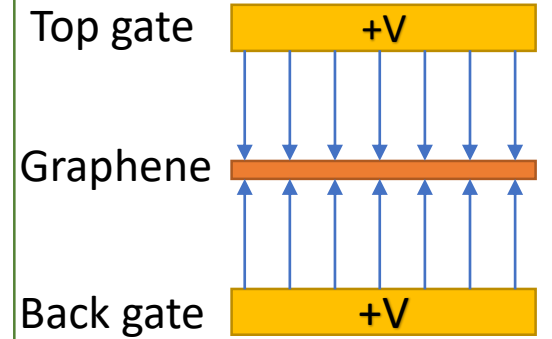


$D=0$

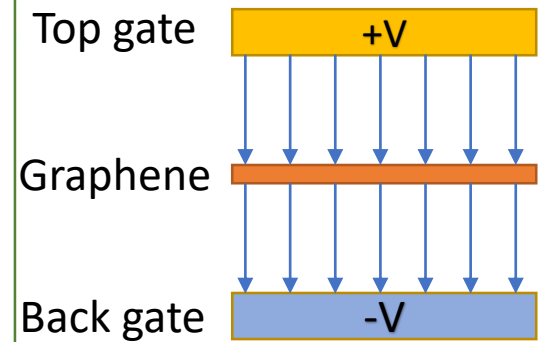
$D \neq 0$

Band structure can be tuned *in situ* with dual-gate geometry, in addition to doping

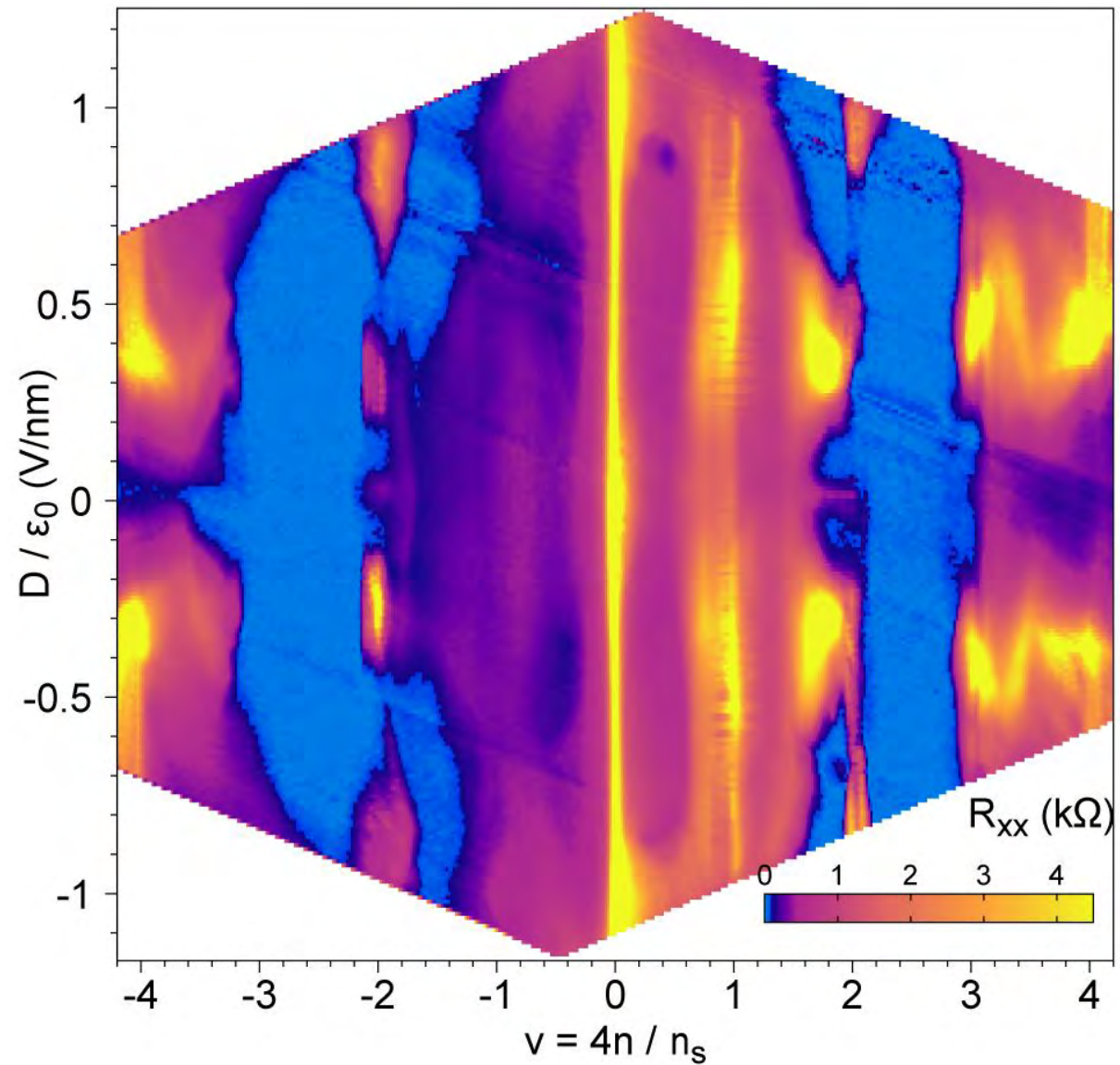
Tuning ν (charge density)



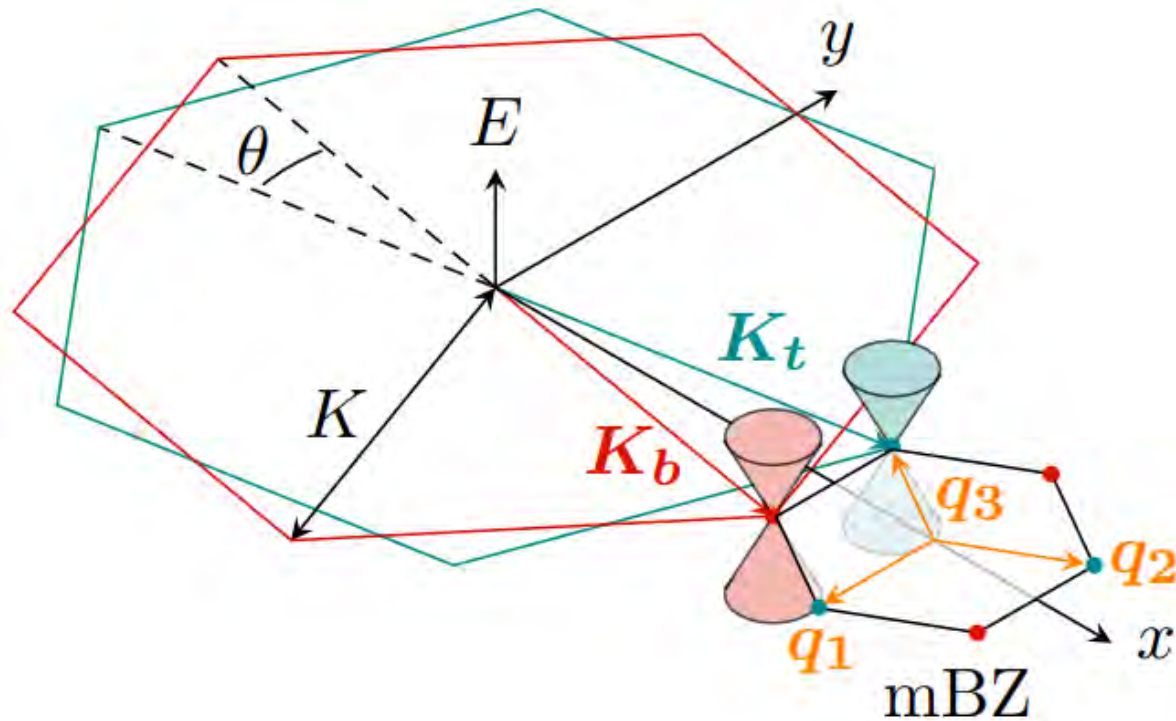
Tuning D (displacement field)



ν - D phase space



Counting electrons in the new BZ

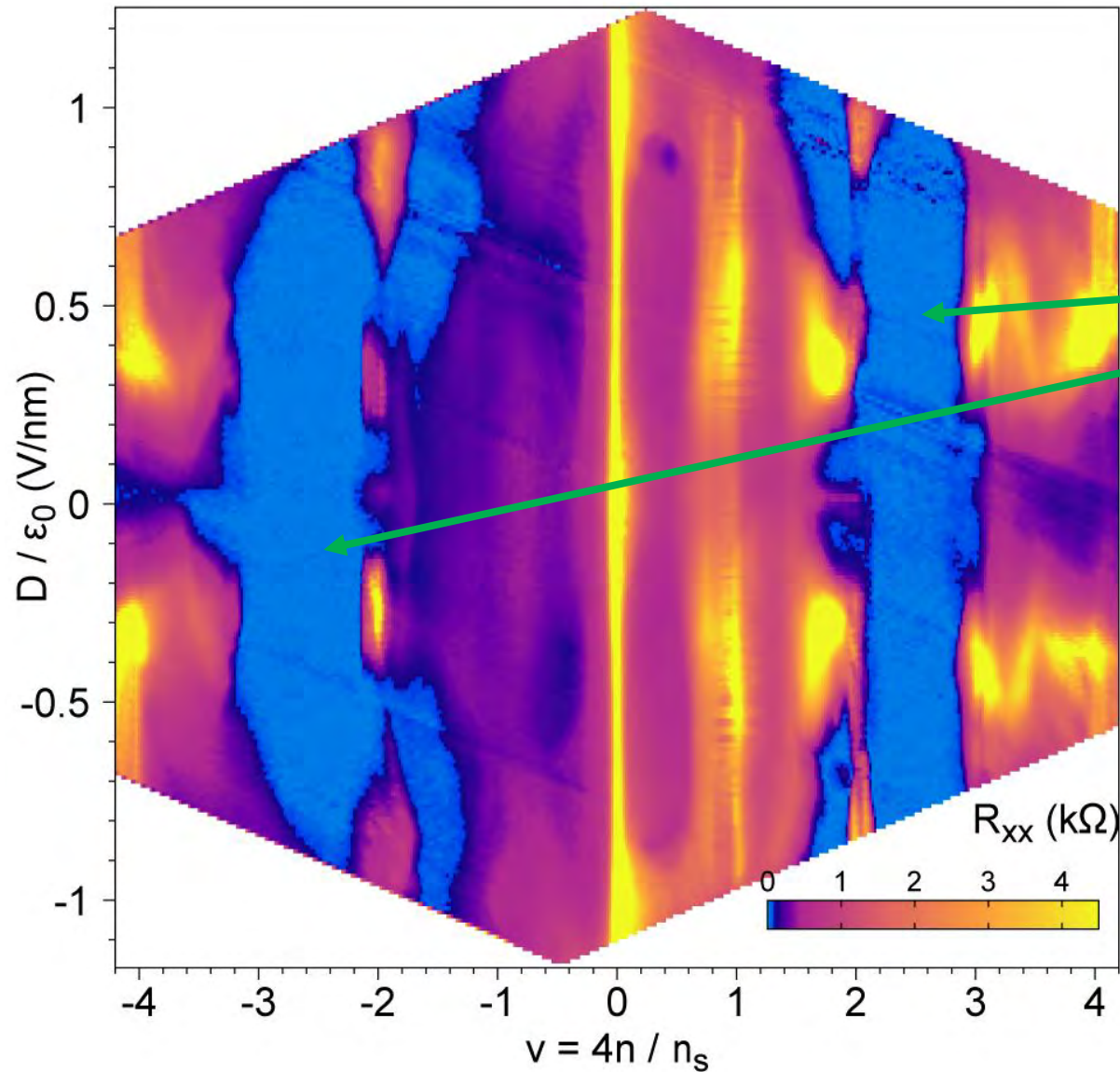


2-fold spin DOF
+
2-fold valley DOF

4-fold spin \times valley “Flavors”

4 electrons per moiré unit cell
to **fill each flat band**

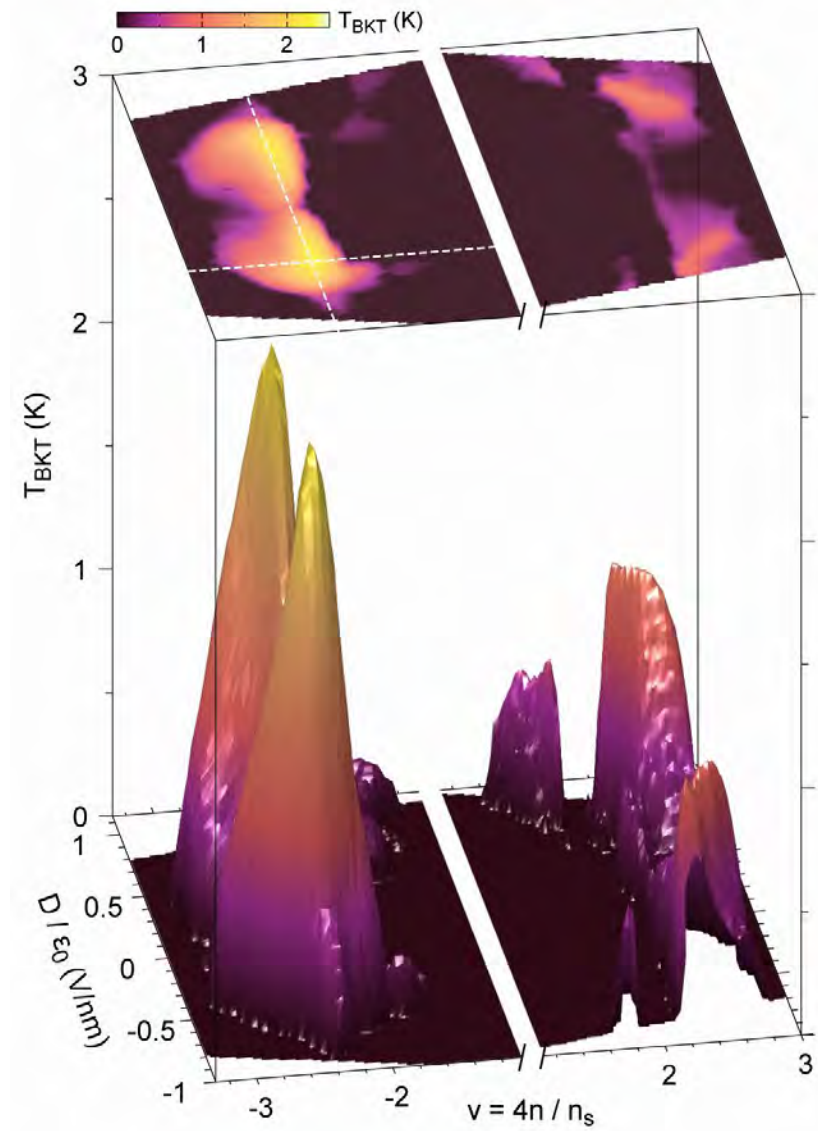
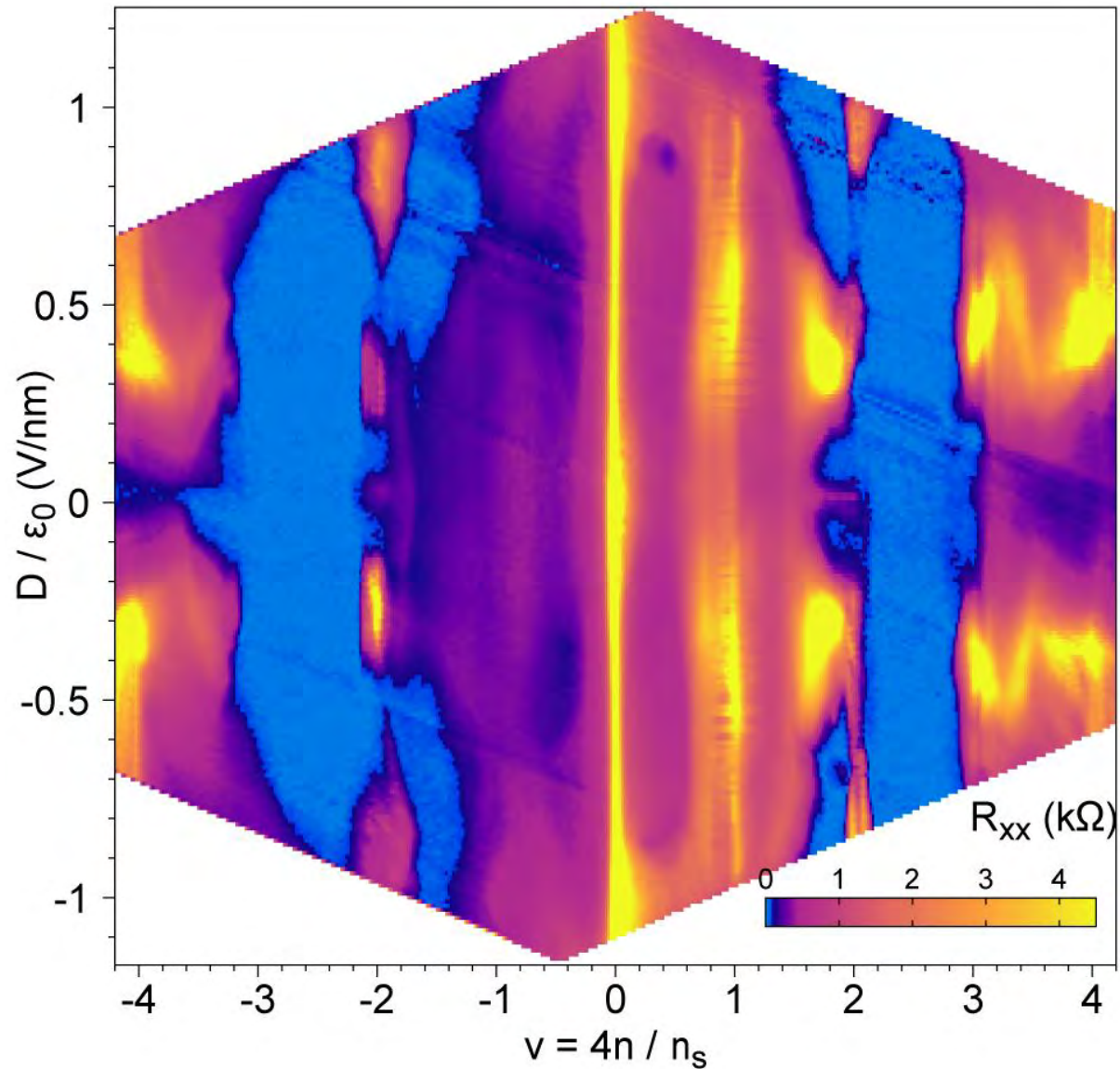
ν - D phase space reveals tunable SC



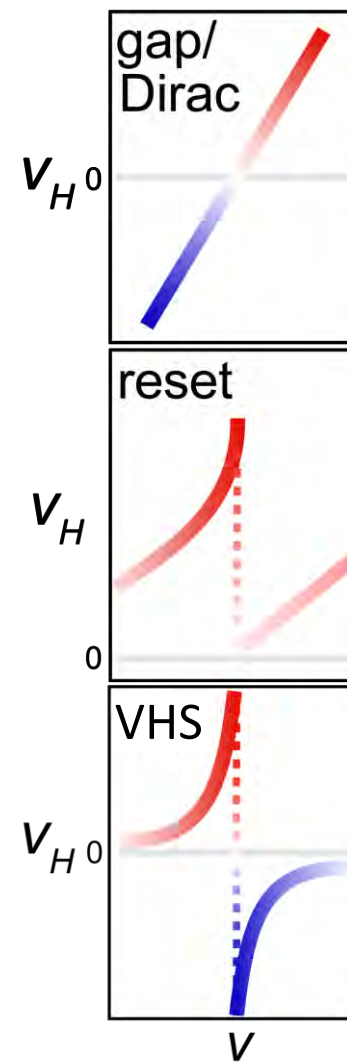
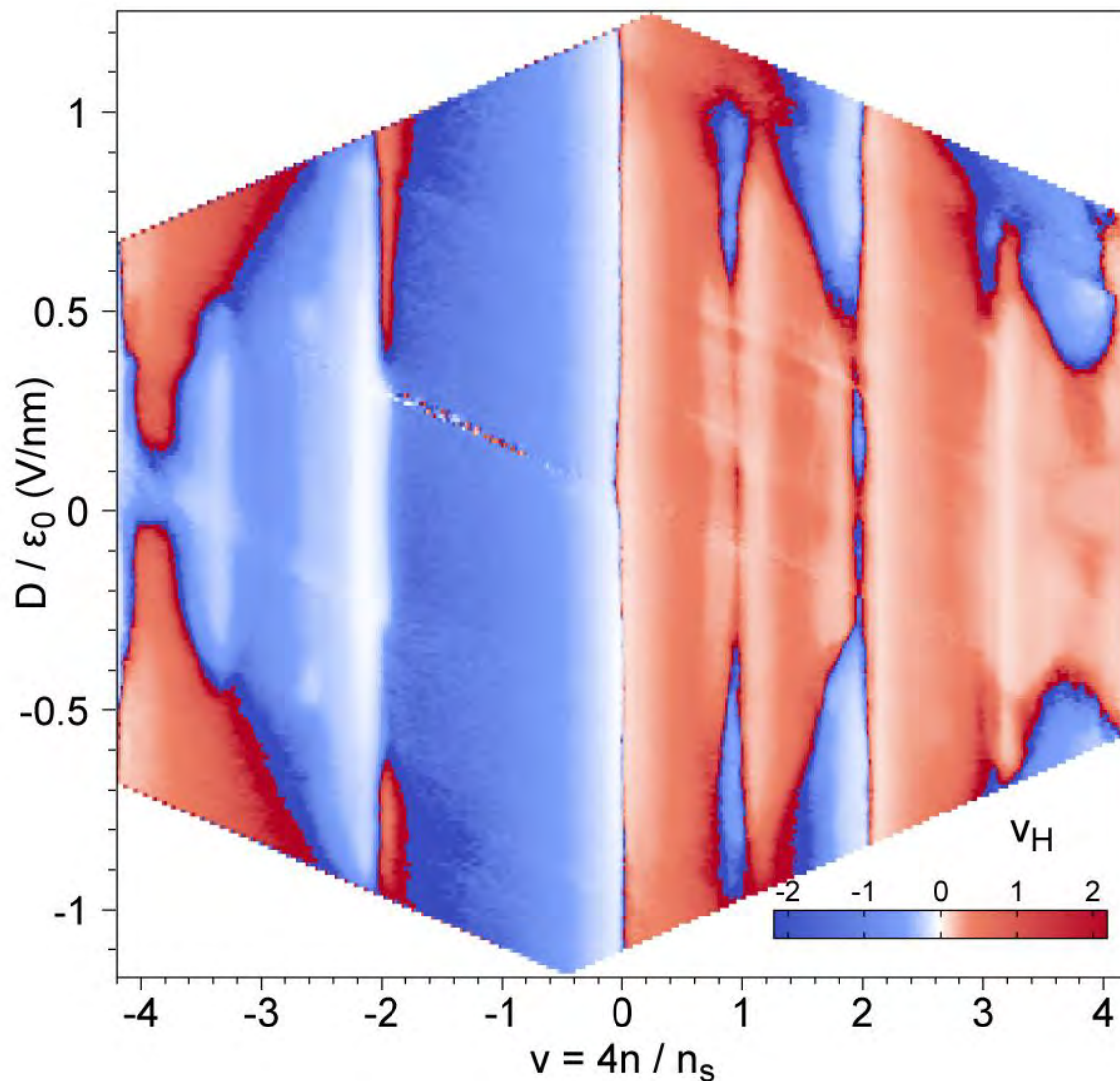
Blue: Superconductivity

Superconductivity exhibits a strong dependence on both ν and D

Tunable superconducting strength

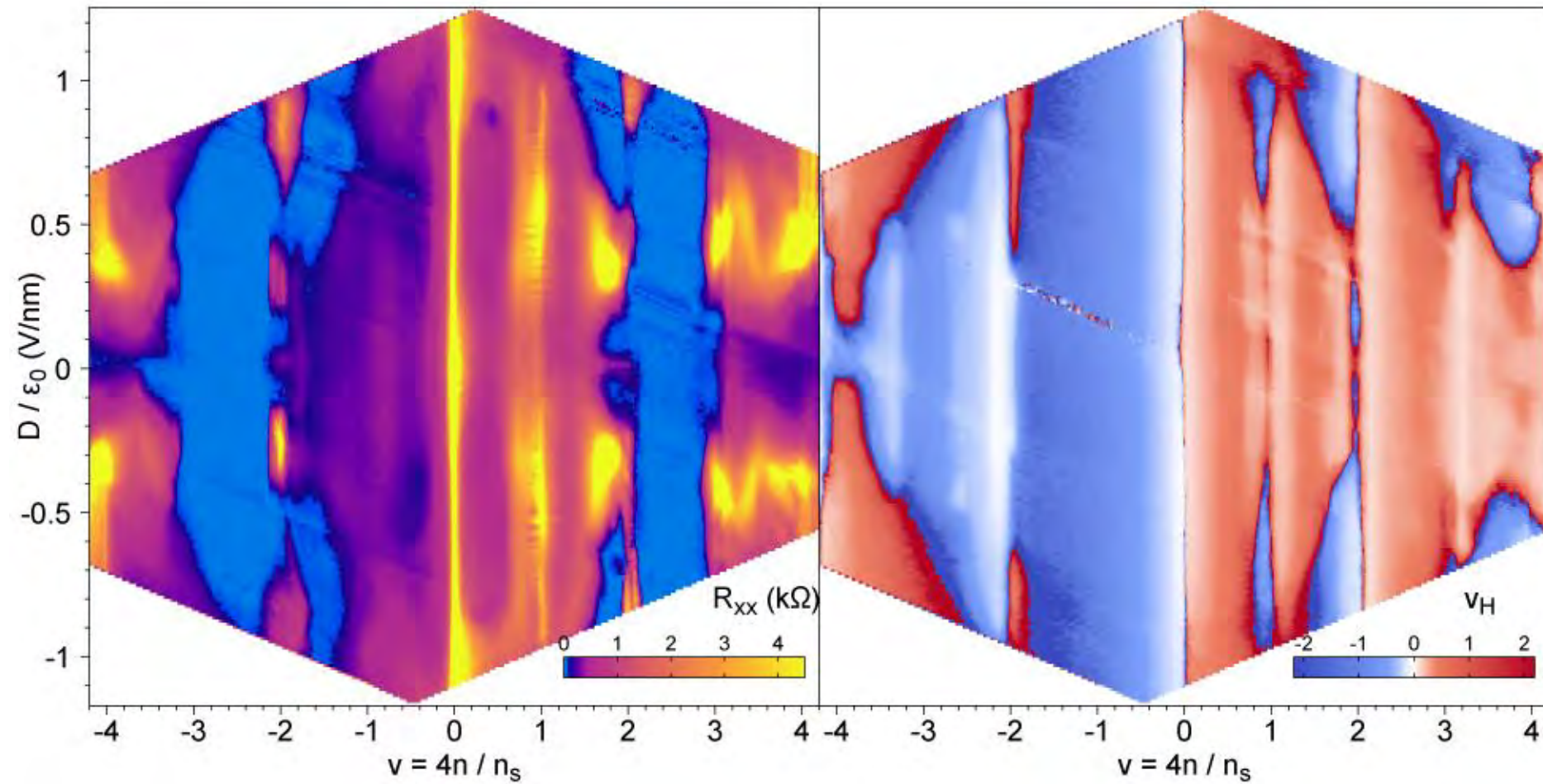


Hall density reveals Fermi surfaces

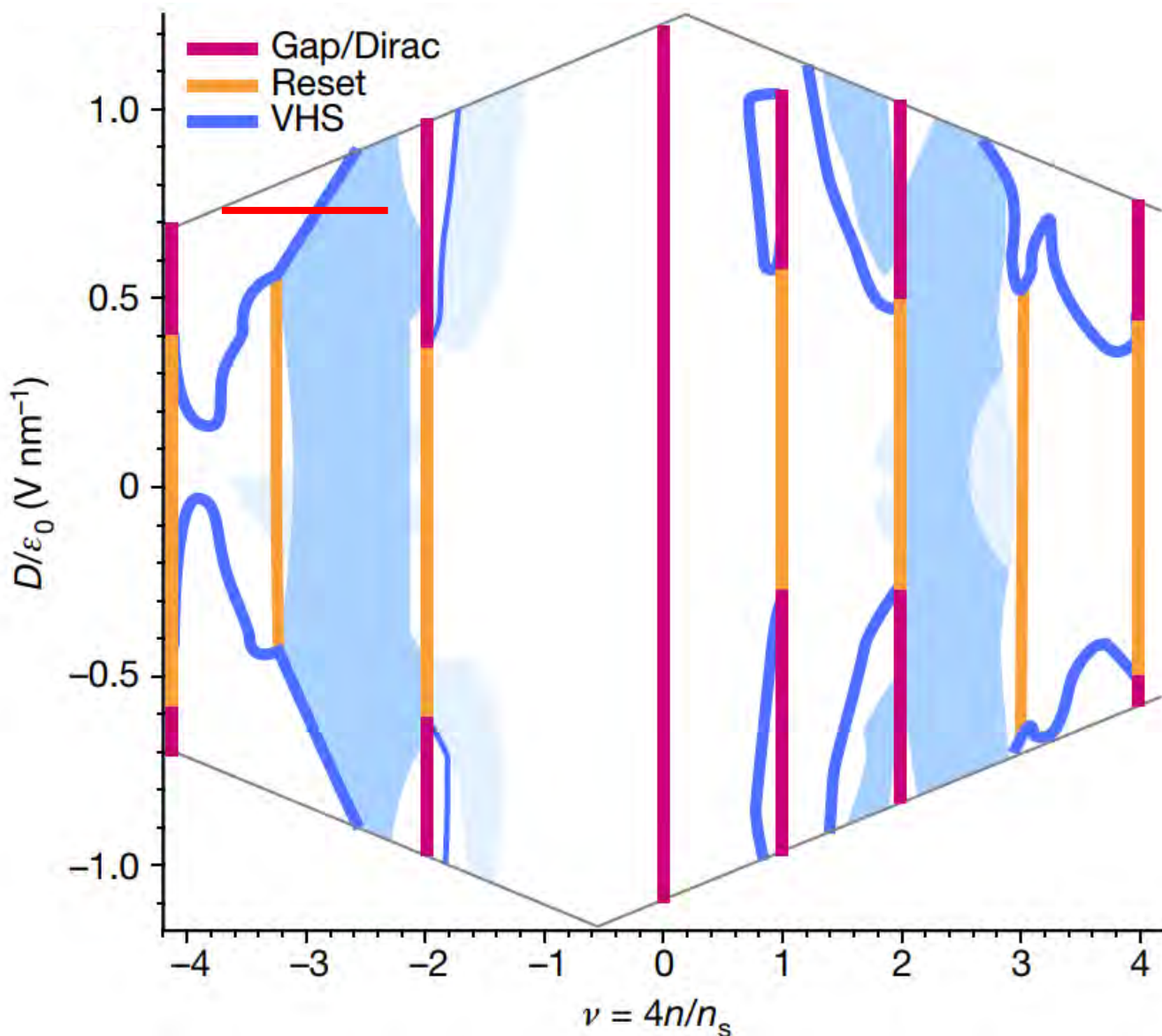


JMP et al. *Nature* **590**, 249 (2021)

Striking similarities

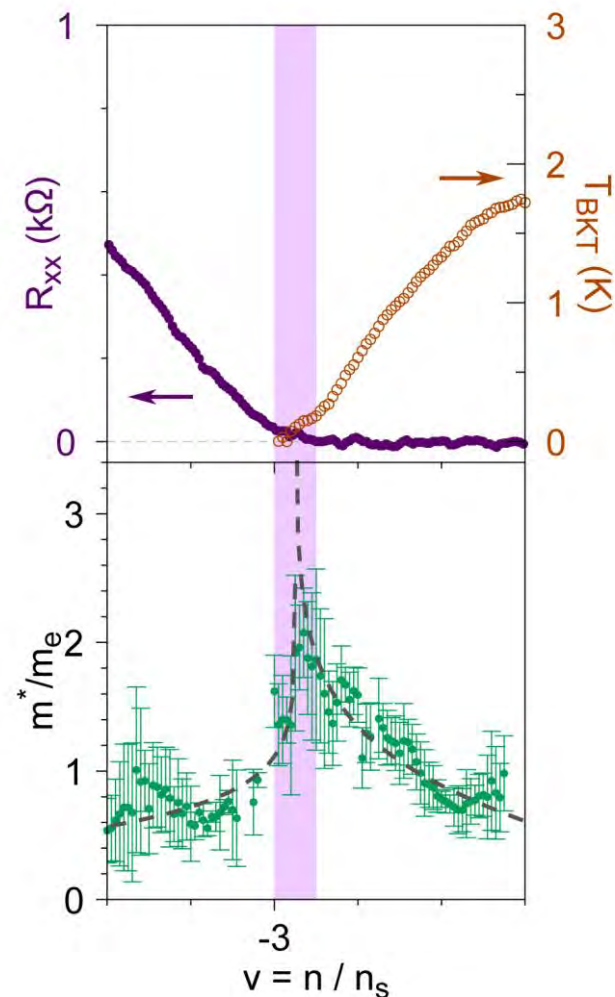


Phase space map reveals unusual SC



Super

Opposite
superconductivity
(BCS)

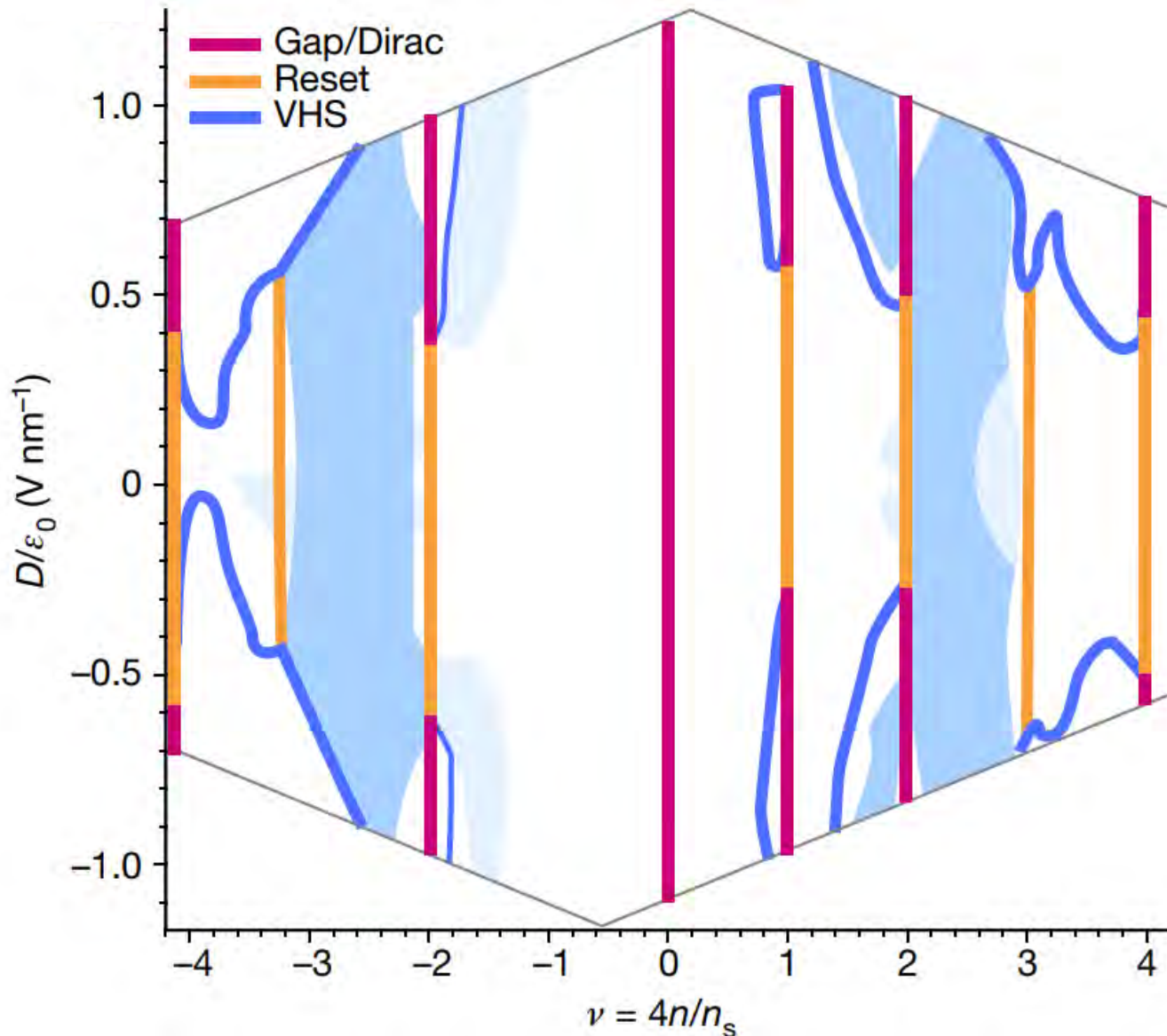


by VHS

BCS

T_c

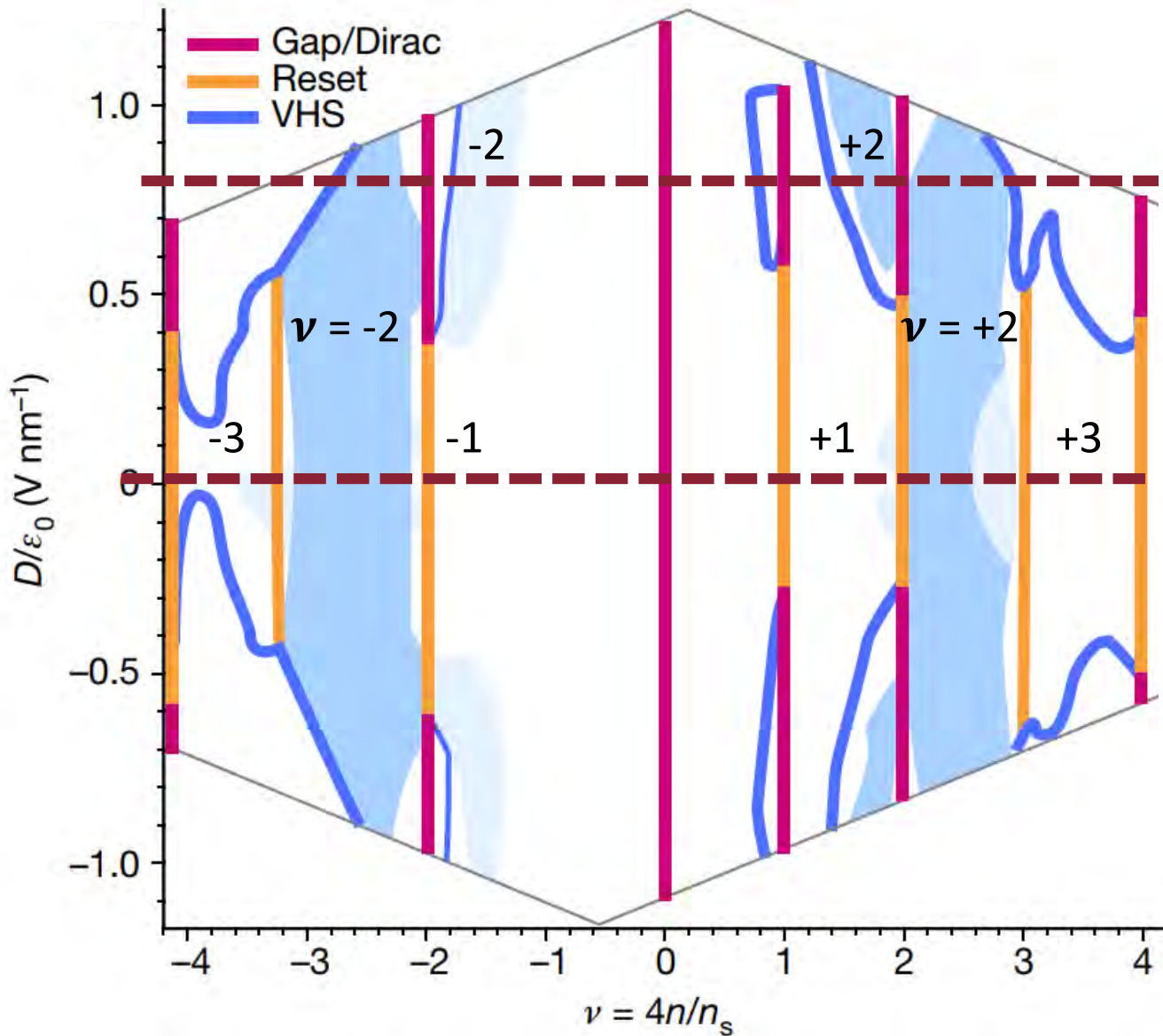
What forms superconductivity?



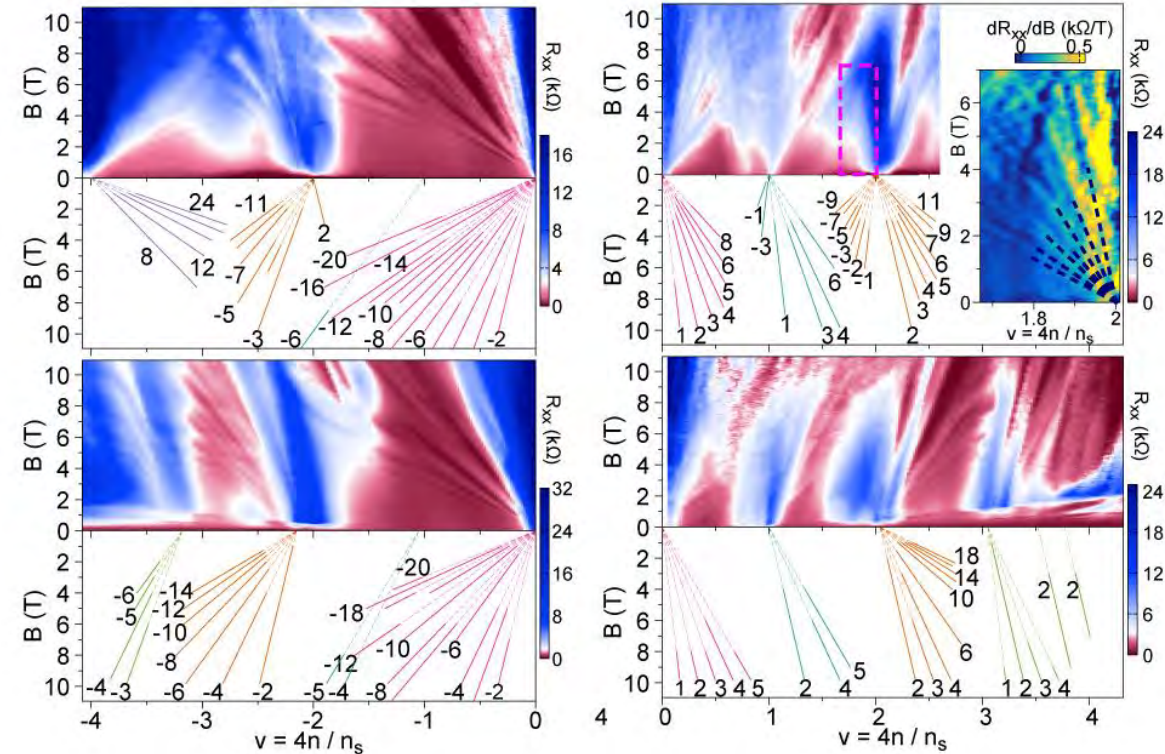
**4-fold spin × valley
flavor symmetry**

Is there symmetry breaking?

SC is from the half-filling broken symmetry states



SC is only from the half-filling carriers!

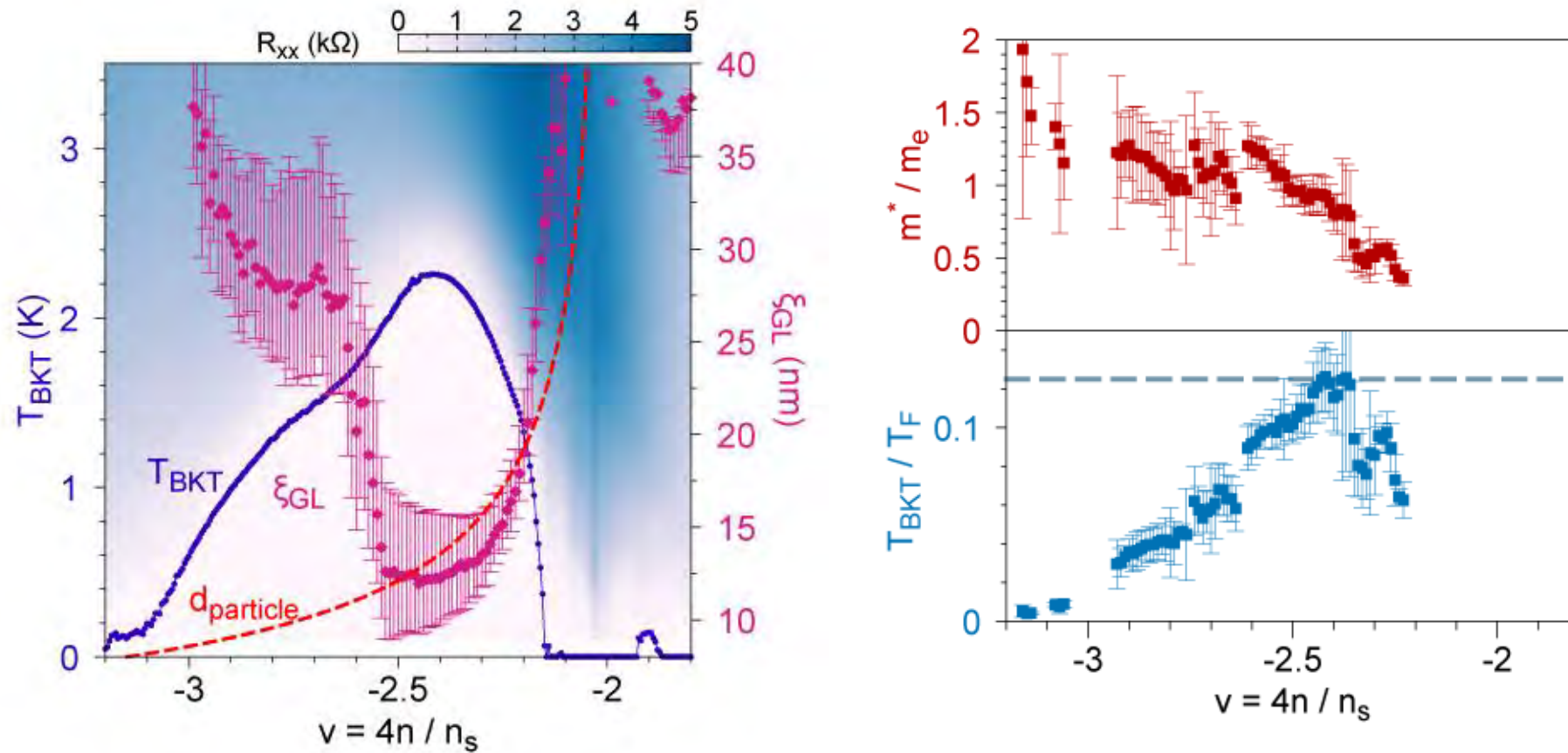


→ Broken symmetry at integer fillings
 → Electronic structures are not the same

JMP et al. *Nature* **590**, 249 (2021)

JMP et al. *Nature* **592**, 43 (2021)

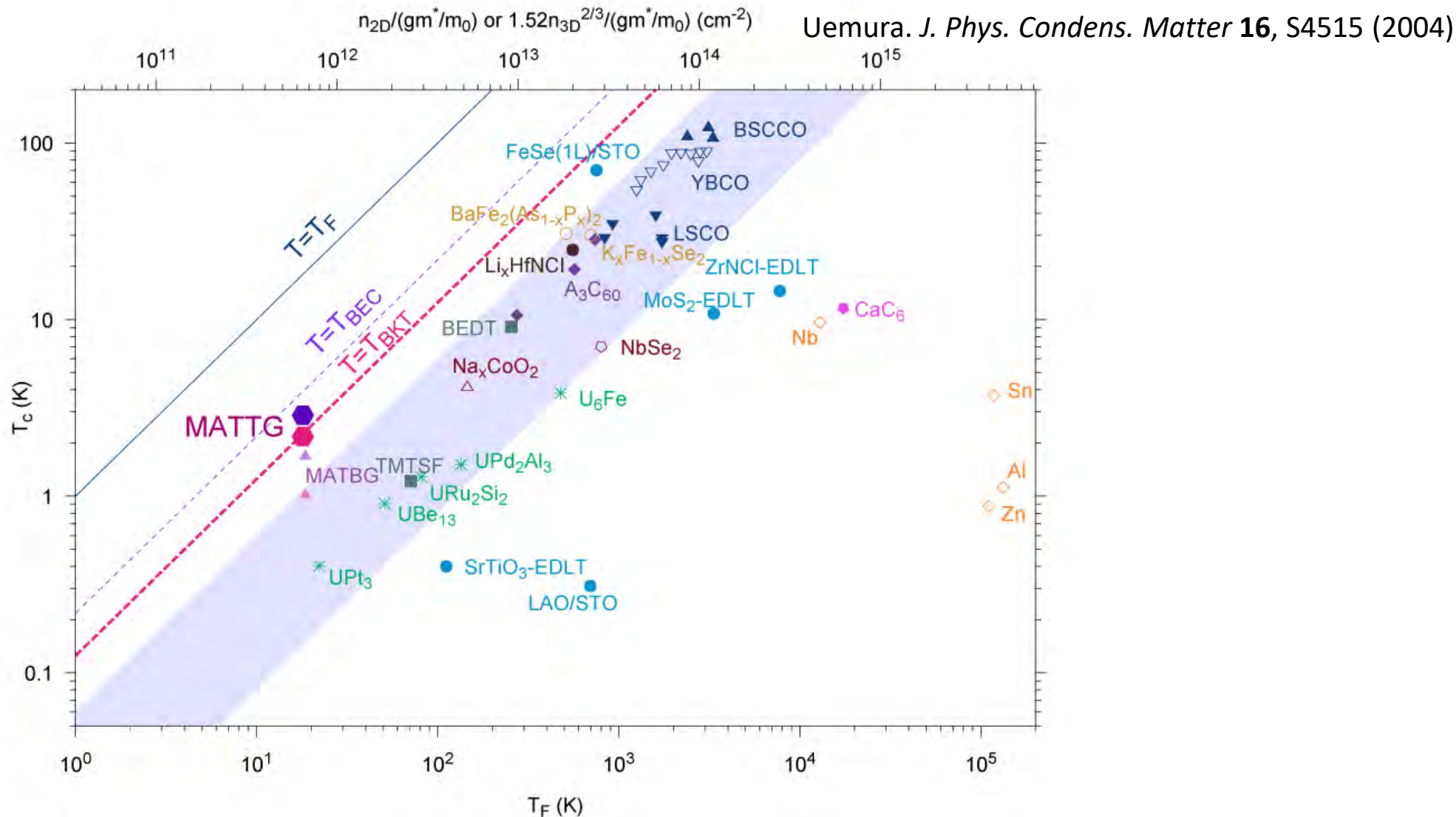
Tunable strongly-coupled superconductivity



Short coherence length: Cooper pair size \lesssim Interparticle distance: **Strongly coupled**

Large $T_{\text{BKT}}/T_F \sim n_{\text{SF}}/n_e$: BCS-BEC crossover regime: **Strongly coupled**

Superconductivity is very strongly coupled!



Our T_c is *high* for such low carrier density – Design principles for future materials

Can we probe the spin structure of SC?

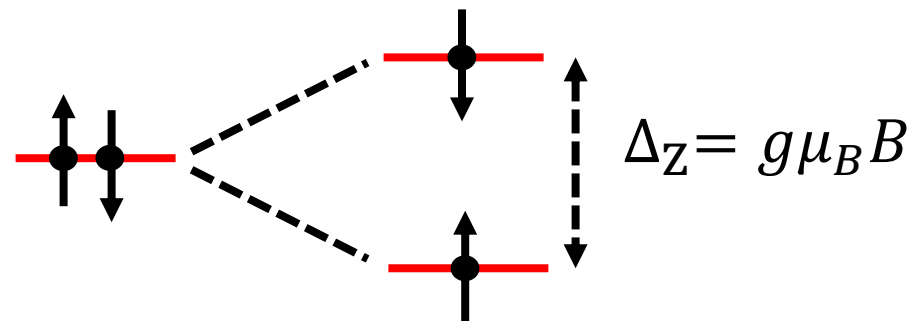


SC wavefunction: (Spatial: s, p, d- wave, etc.) x (Spin: singlet, triplet, etc.)

Spin-singlet Cooper Pairs $\frac{1}{\sqrt{2}}(|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle)$

Binding energy (BCS) $\Delta_{\text{BCS}} = 1.76k_B T_C$

Zeeman effect “breaks” Cooper pairs apart

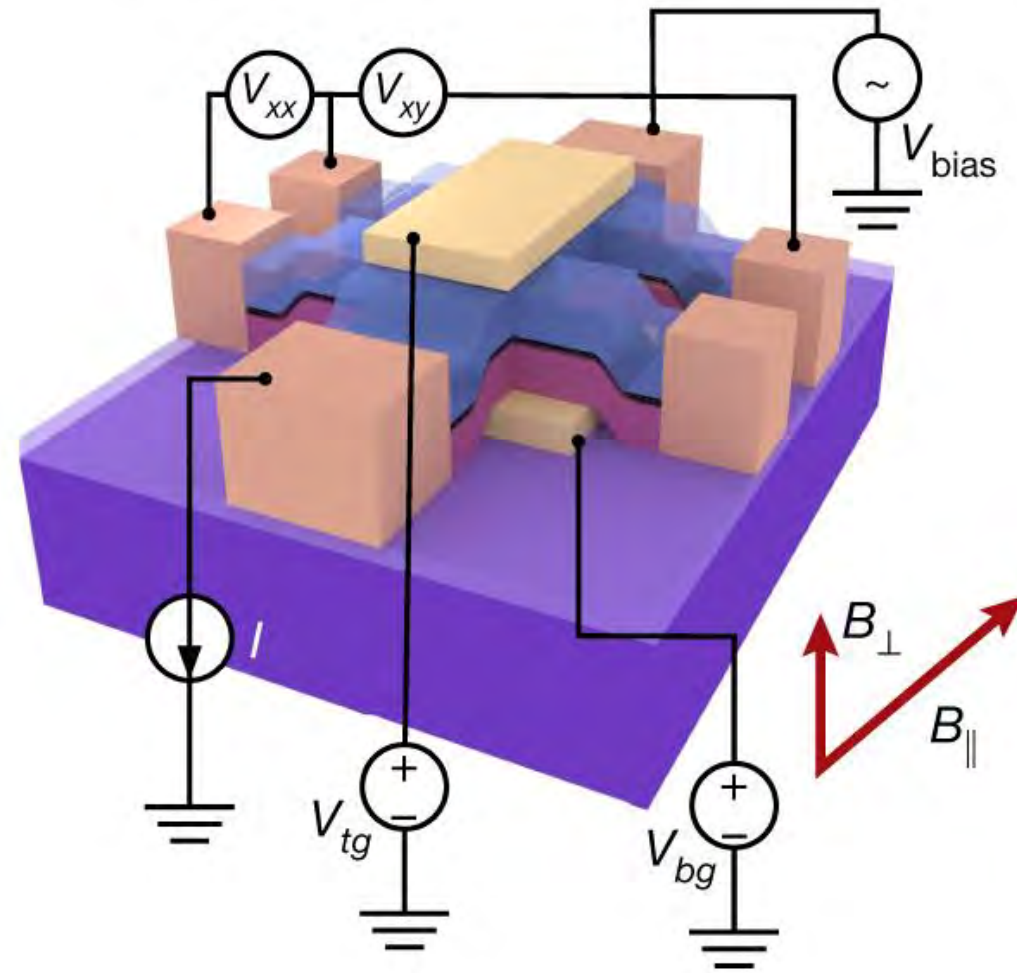


Pauli limit (paramagnetic limit, Chandrasekhar-Clogston limit):

$$B_p = 1.86 \frac{\text{T}}{\text{K}} \times T_c \quad (\text{e.g. } B_p = 1.86\text{T for } T_c = 1\text{K})$$

for BCS spin-singlet superconductors

Can we probe the spin structure of SC?



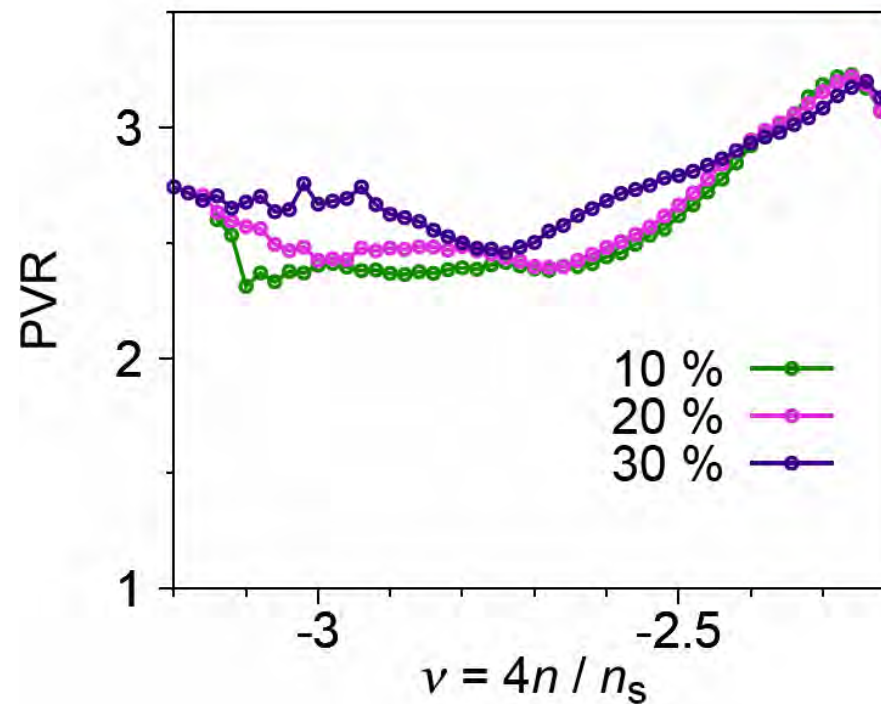
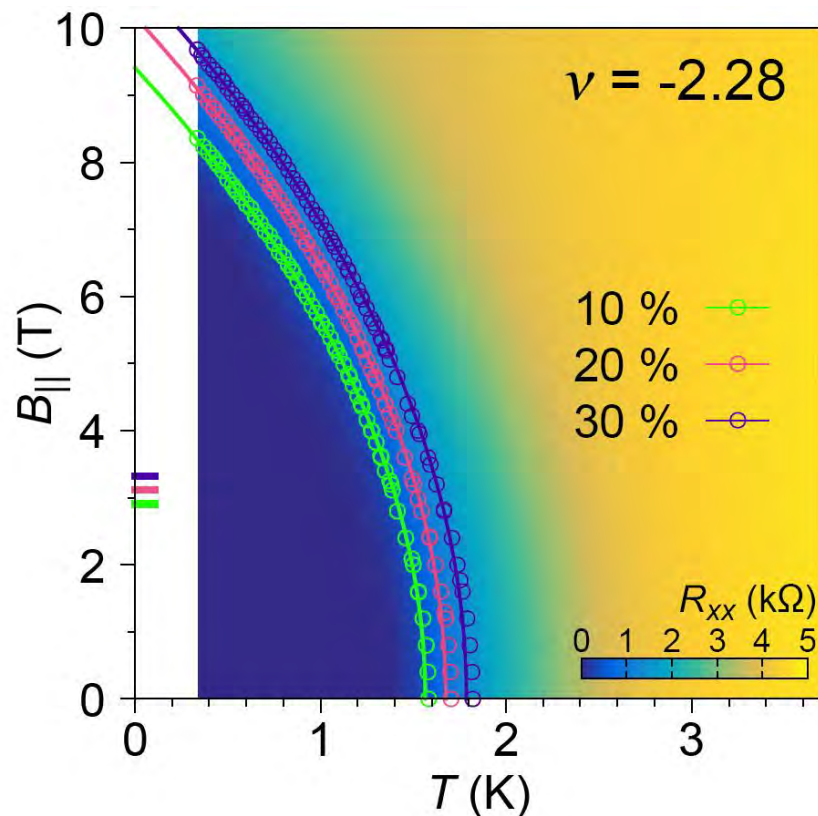
Pauli limit is violated in MATTG



Pauli limit (paramagnetic limit, Chandrasekhar-Clogston limit):

$$B_P = 1.86 \frac{T}{K} \times T_C \quad (\text{e.g. } B_P = 1.86\text{T for } T_C = 1\text{K})$$

for BCS spin-singlet superconductors



JMP et al. *Nature* **590**, 249 (2021)
Cao*, JMP* et al. *Nature* **595**, 526 (2021)

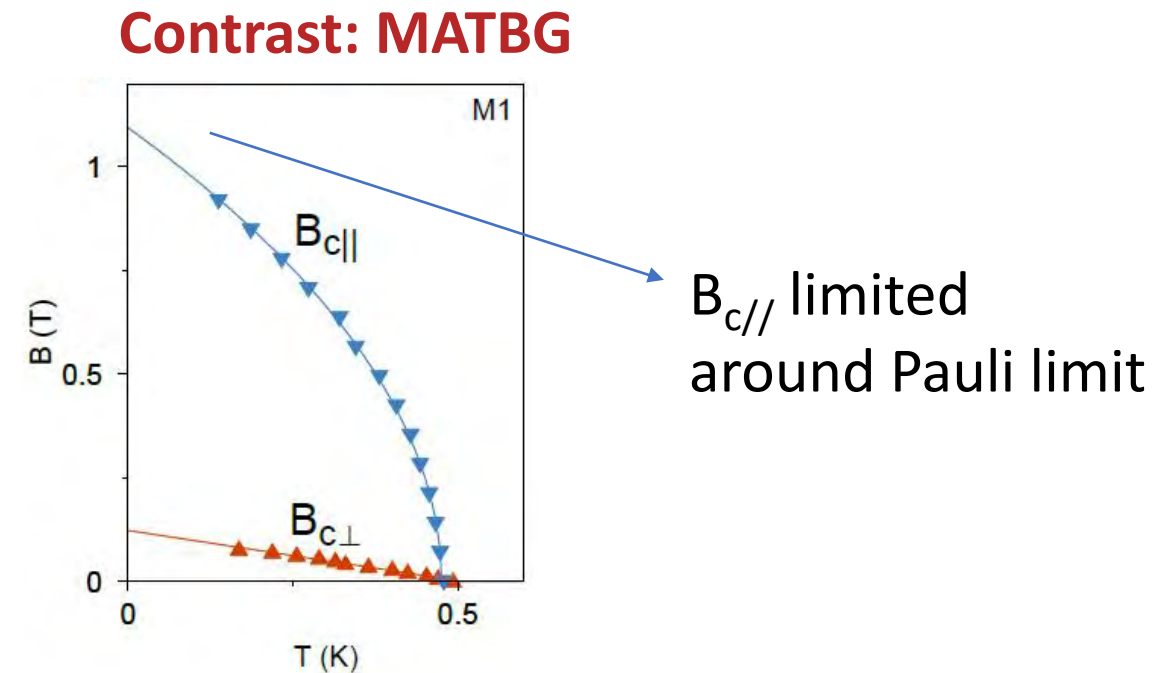
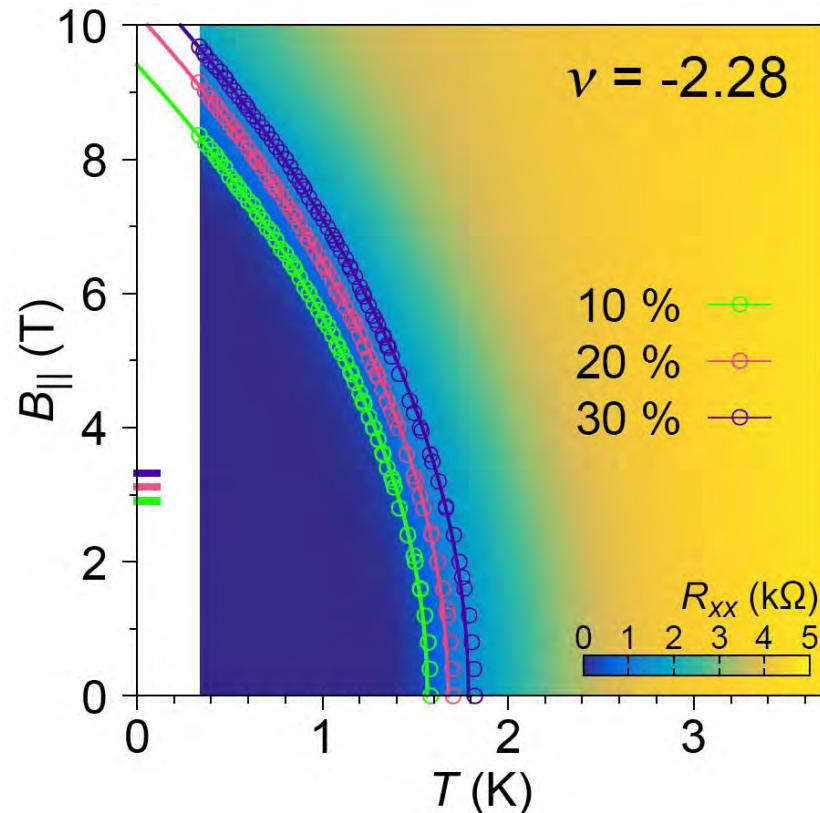
Pauli limit is not violated in MATBG



Pauli limit (paramagnetic limit, Chandrasekhar-Clogston limit):

$$B_P = 1.86 \frac{\text{T}}{\text{K}} \times T_C \quad (\text{e.g. } B_P = 1.86\text{T for } T_C = 1\text{K})$$

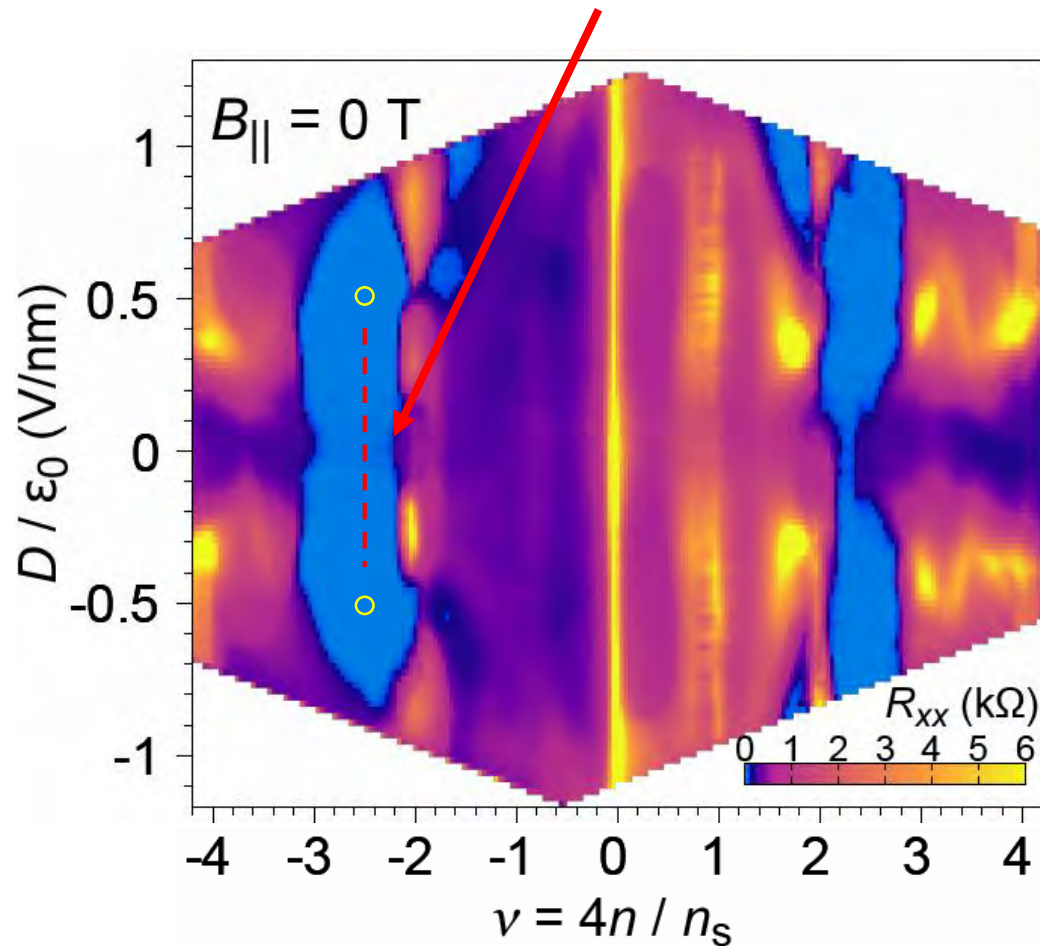
for BCS spin-singlet superconductors



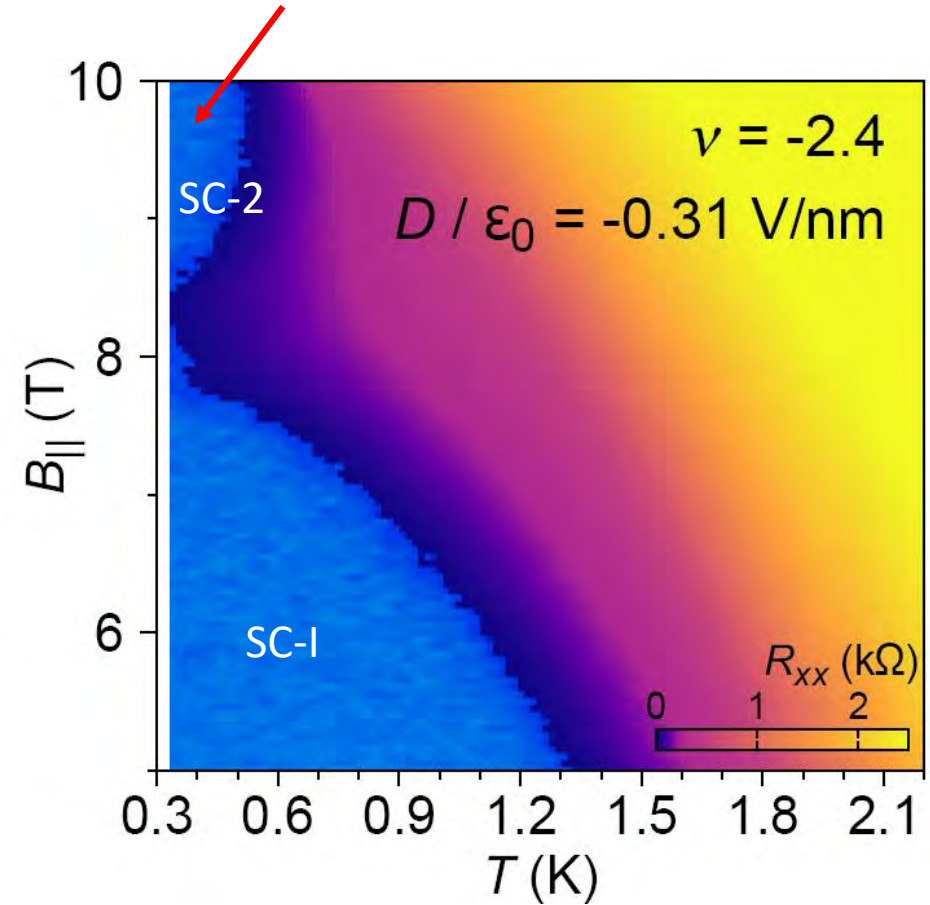
Reentrant superconductivity in MATTG



At a different displacement field...



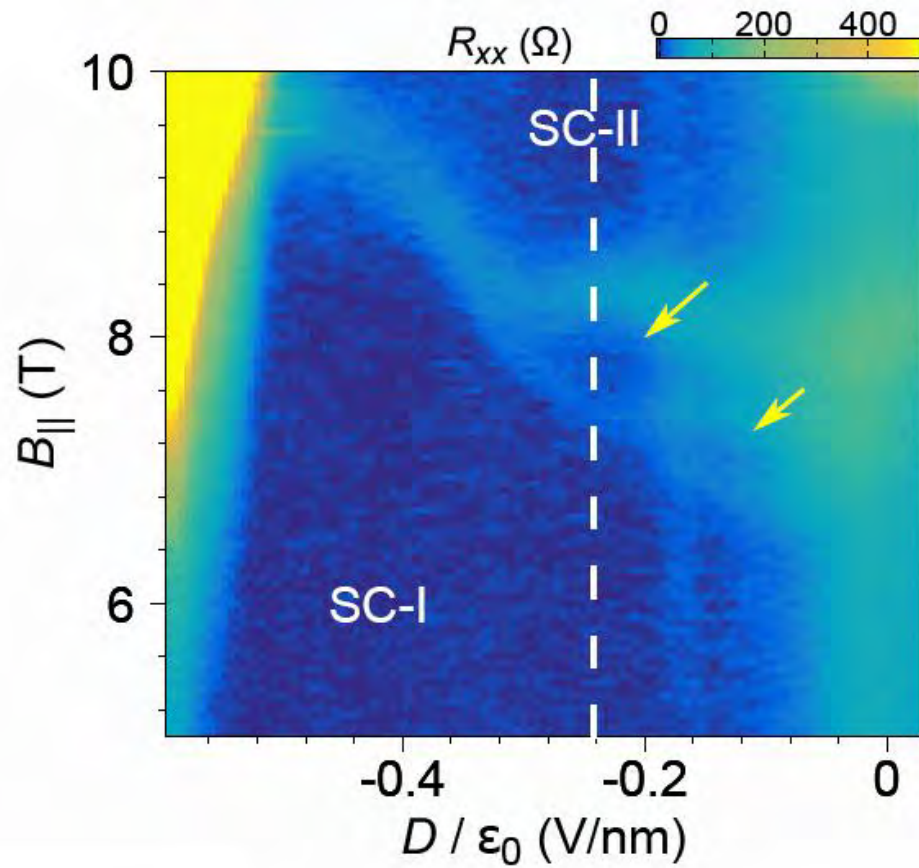
Reentrant superconductivity at high B



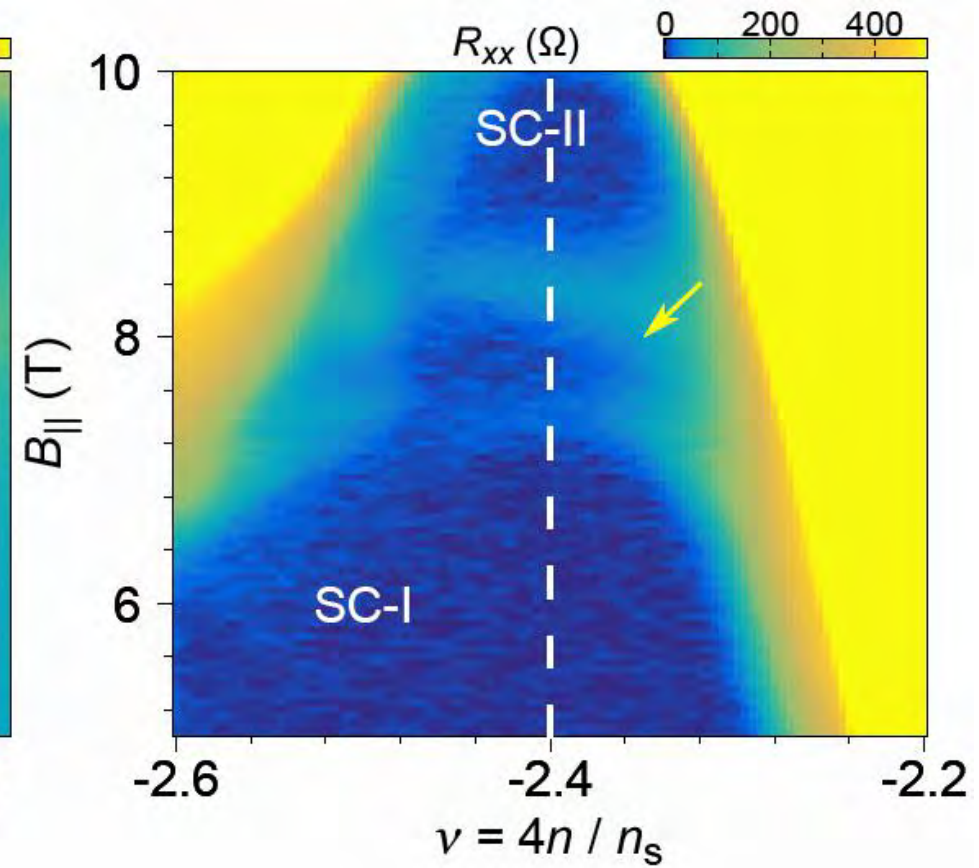
Tunable reentrant superconductivity



Displacement field

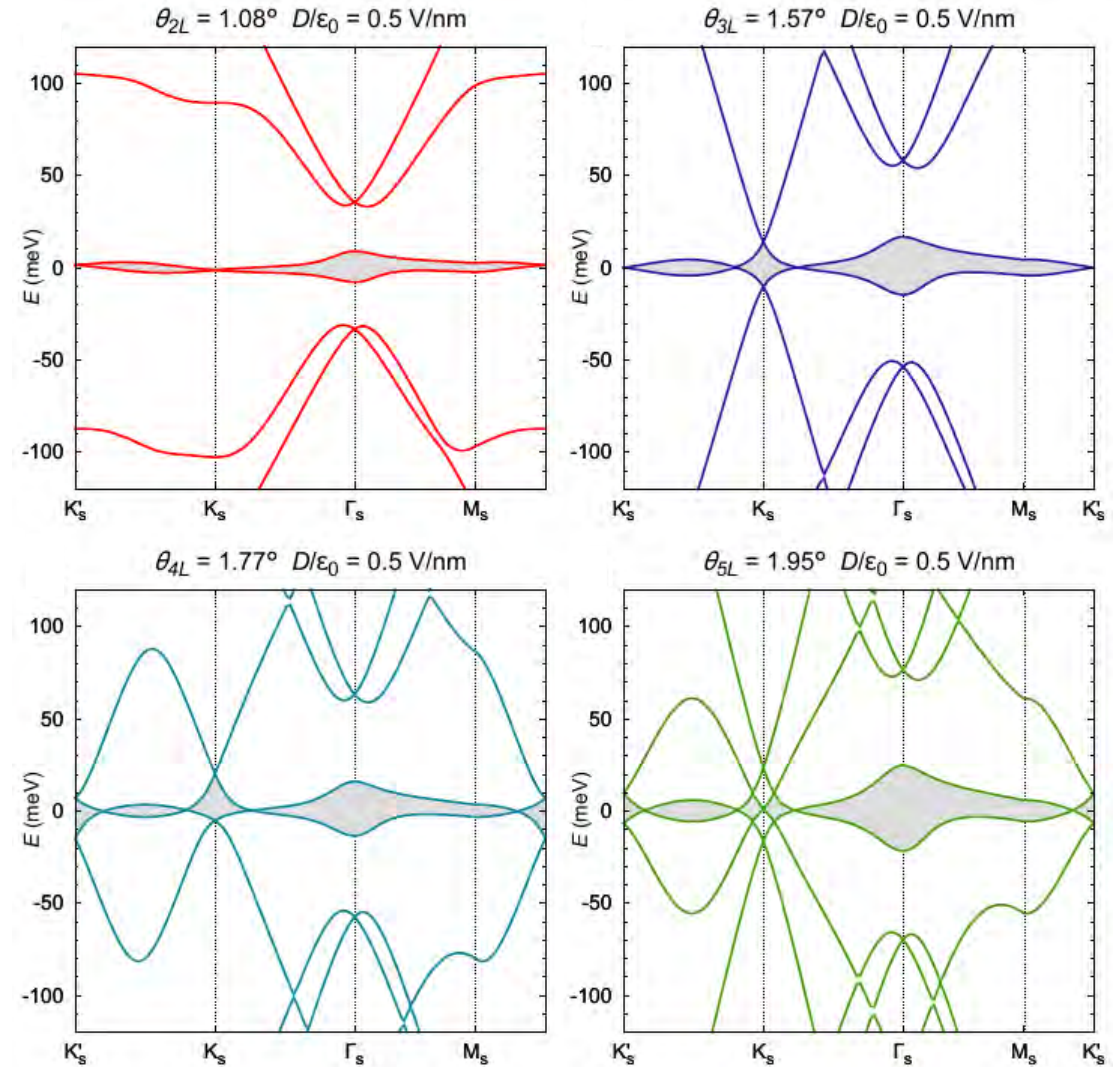
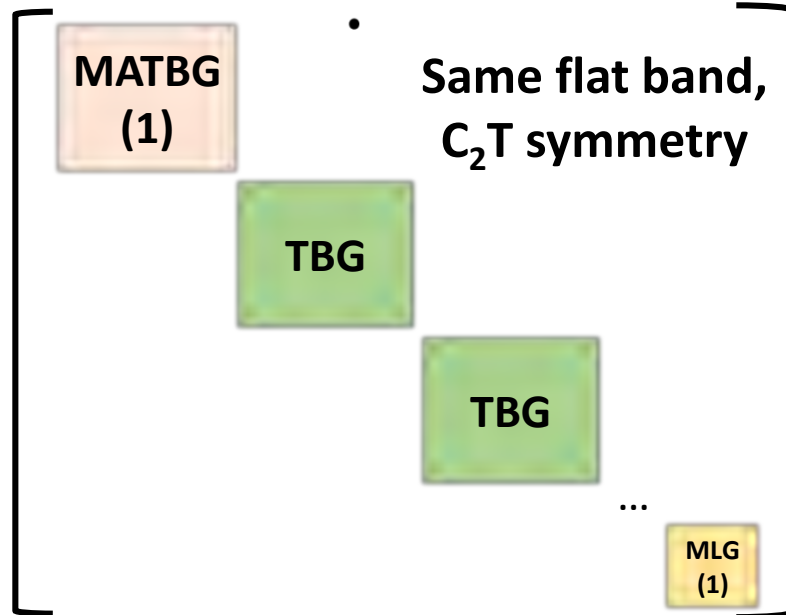
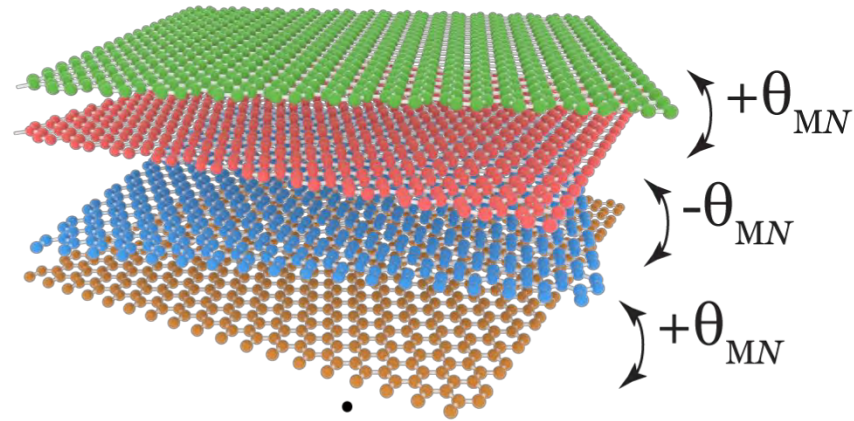


Doping

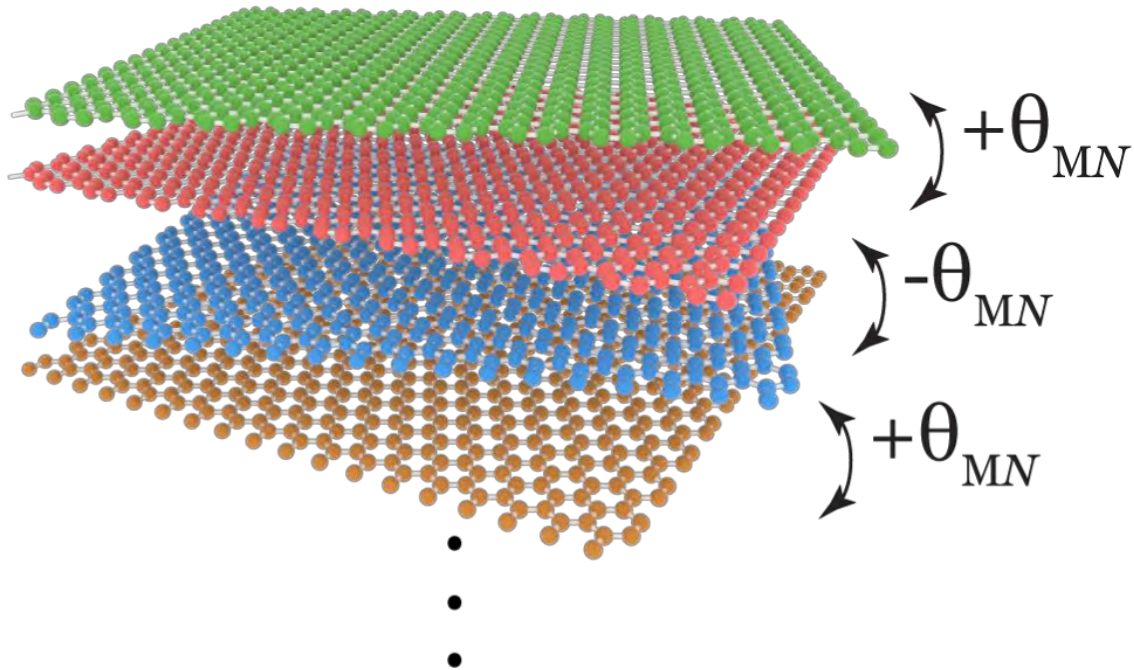


- 2-dimensional materials for strongly correlated physics
 - Magic-angle twisted bilayer graphene
- Magic-angle twisted trilayer graphene
- **The magic family**
- Outlook

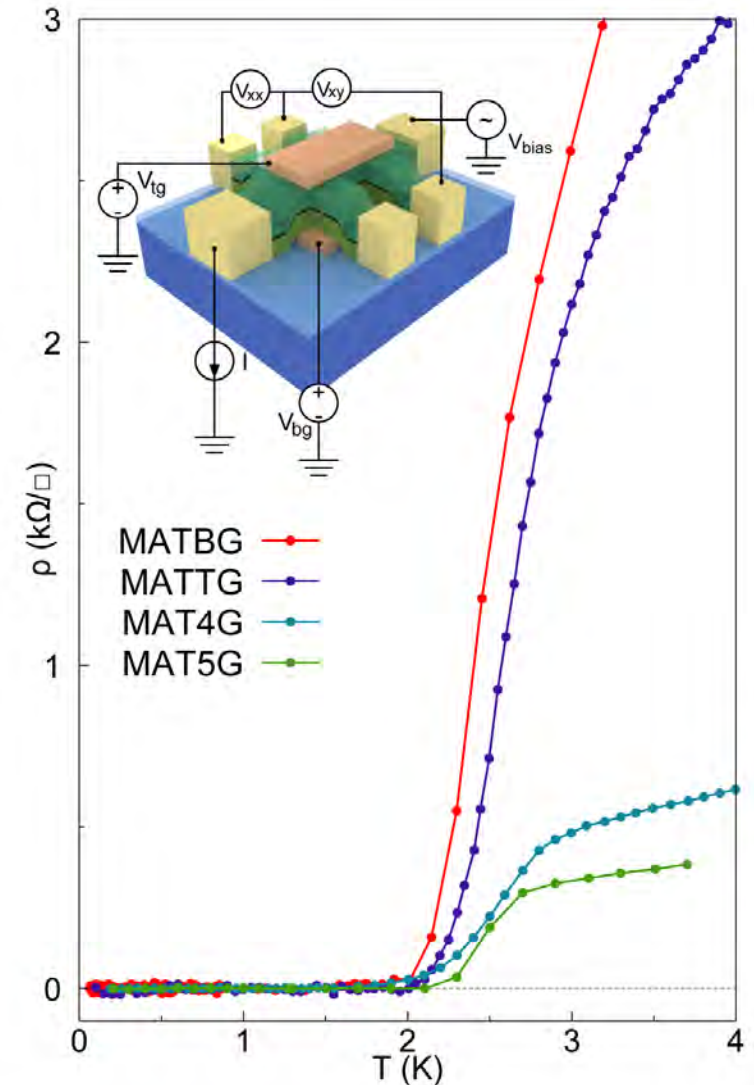
The magic extends!



The magic family of robust superconductors



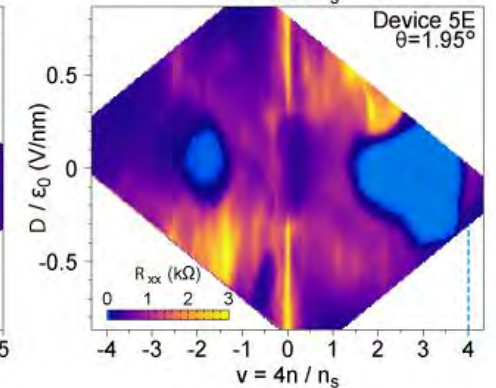
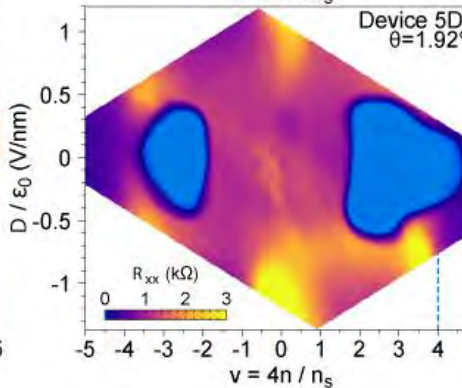
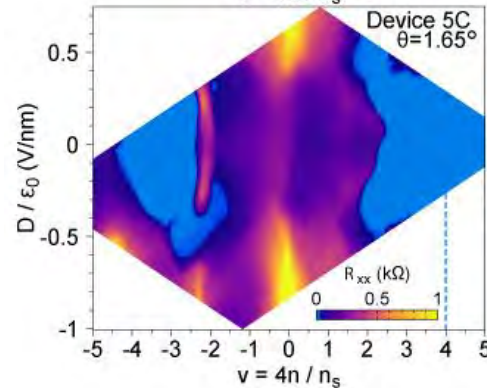
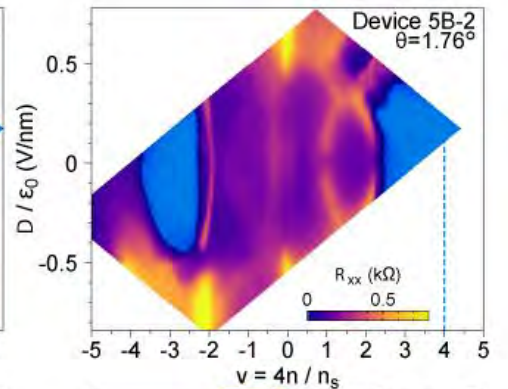
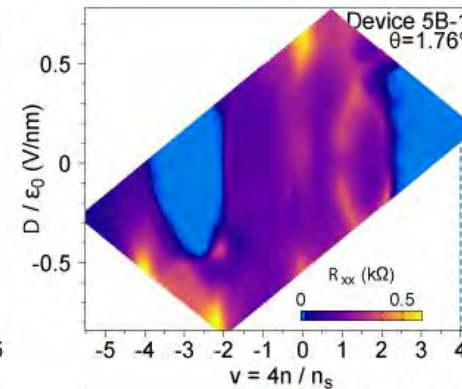
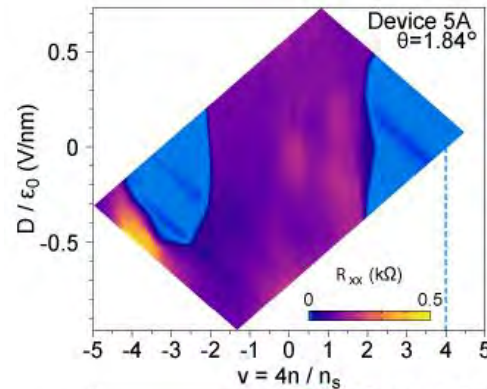
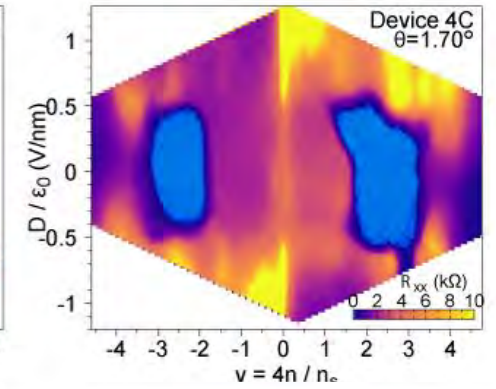
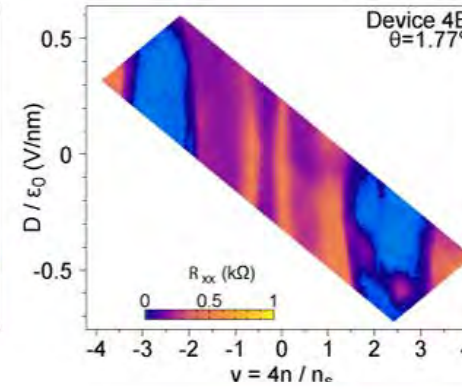
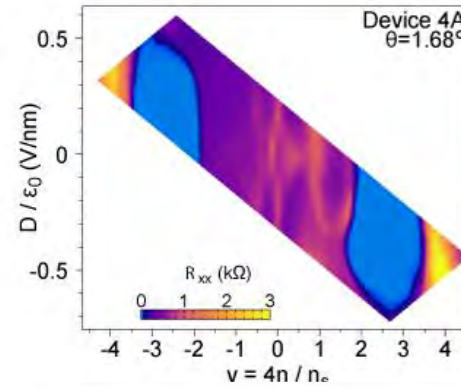
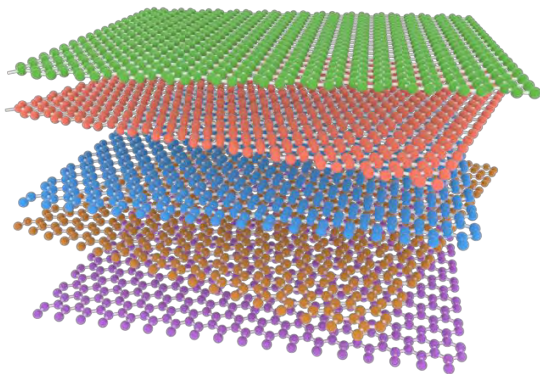
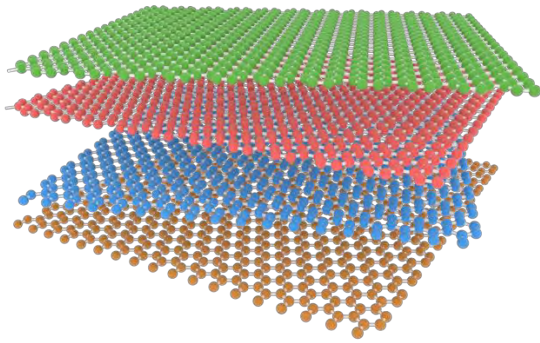
Family of strongly-coupled superconductors!



See also: Nadj-Perge Group. *Science* **377**, 1538 (2022)

JMP et al. *Nature Materials* **21**, 877 (2022)

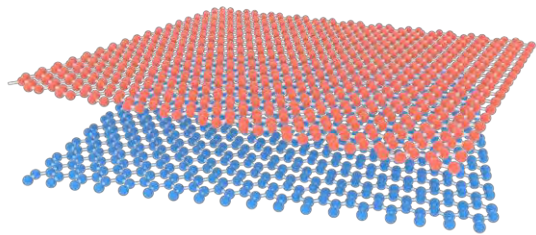
~100% magic rate



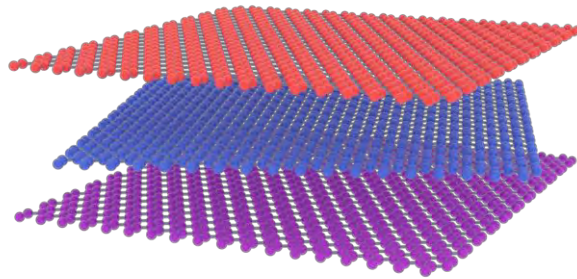
The magic family



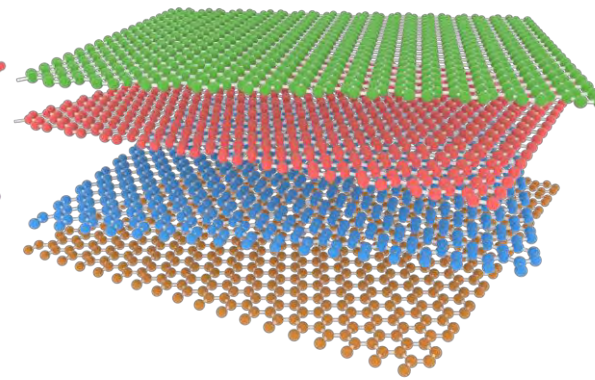
2L



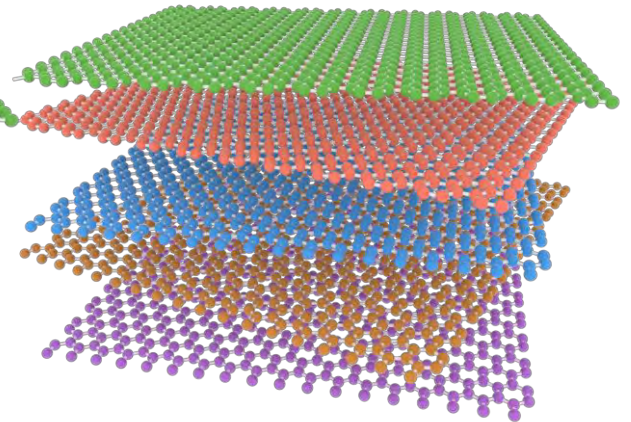
3L



4L



5L



Pauli limit violation

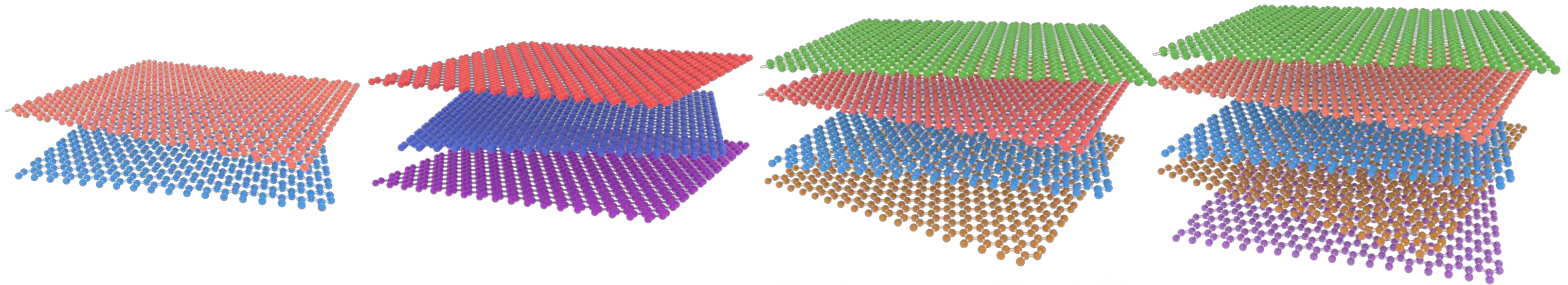


2L

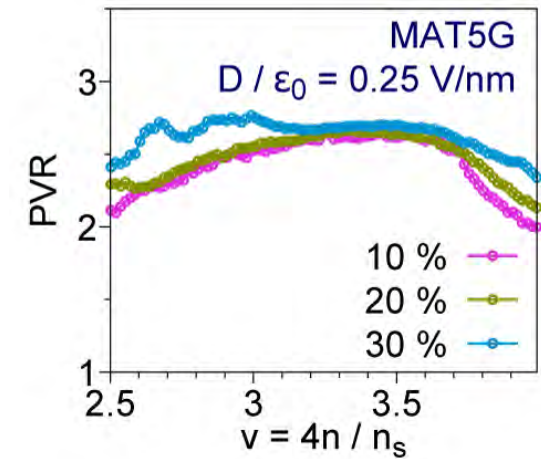
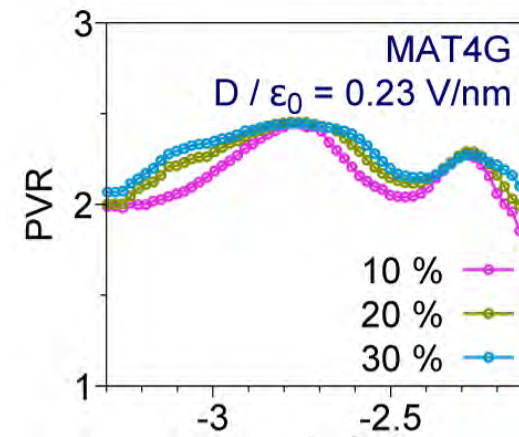
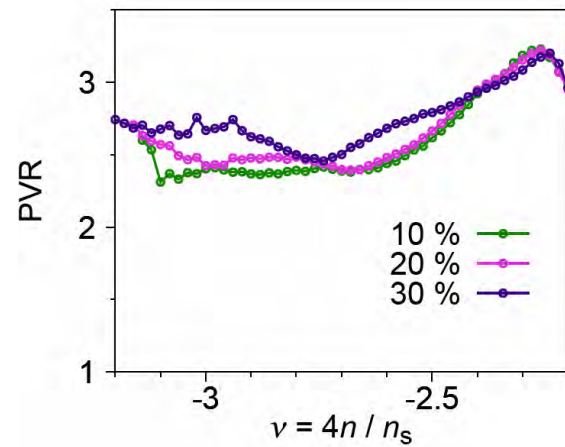
3L

4L

5L

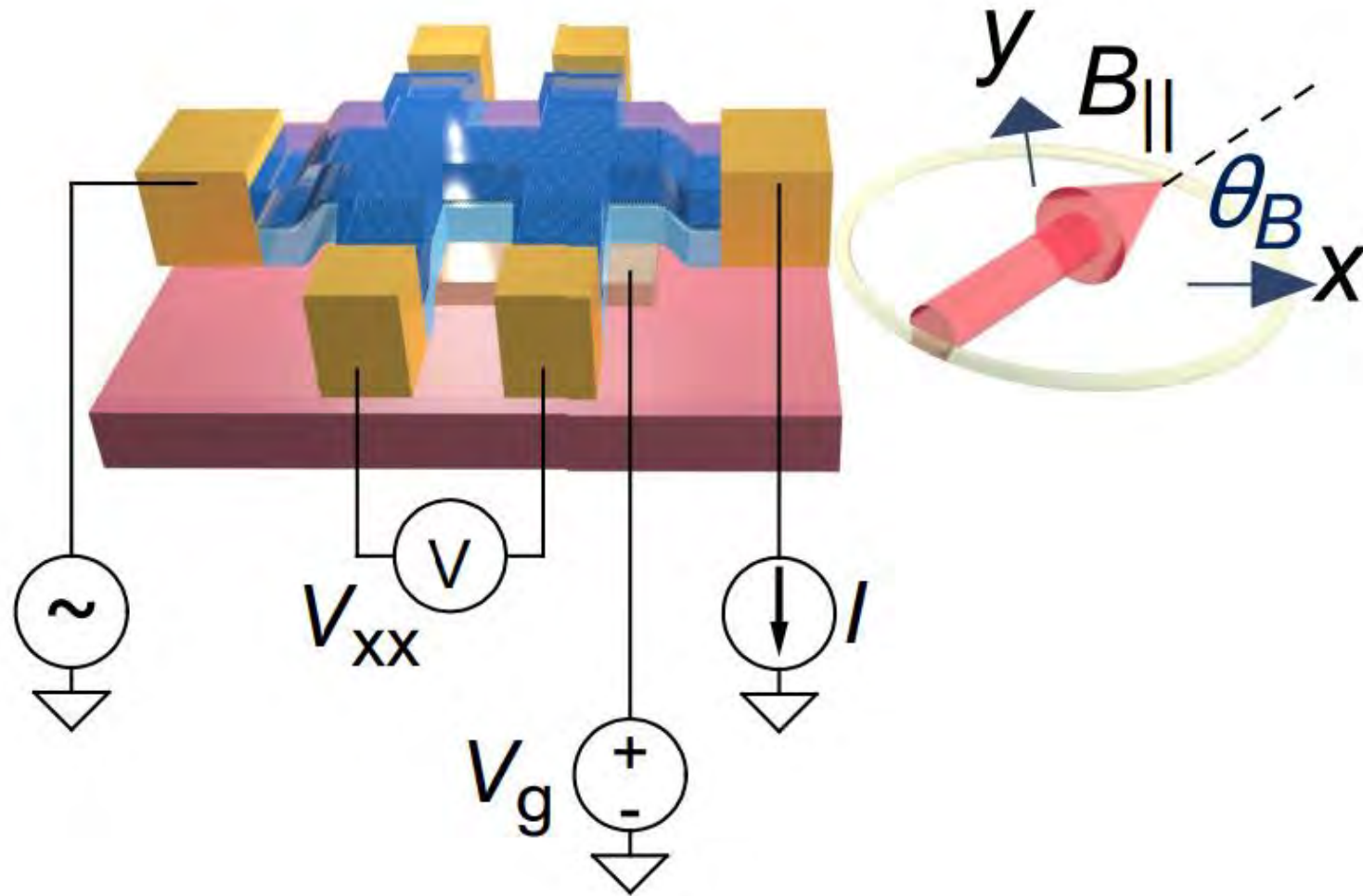


Not violating
the Pauli limit



Only 3-5L consistently violate the Pauli limit

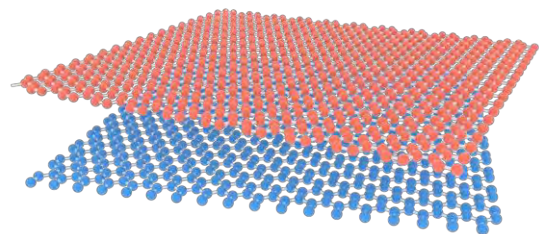
Angle-dependent magnetic field response



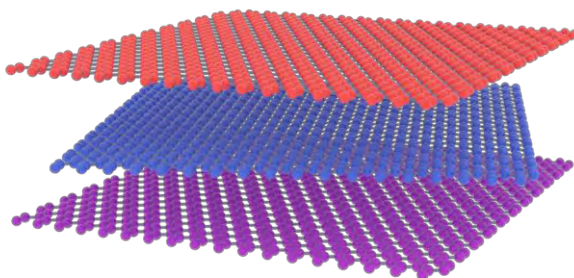
Spontaneous breaking of rotational symmetry



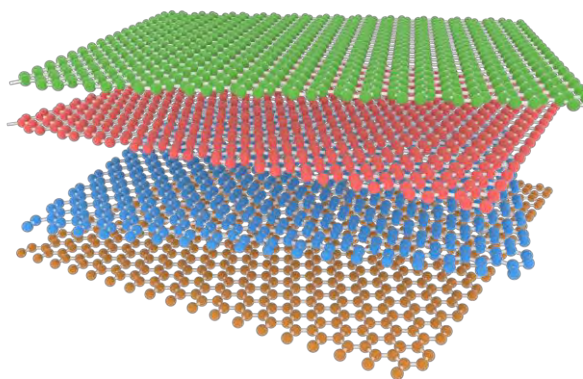
2L



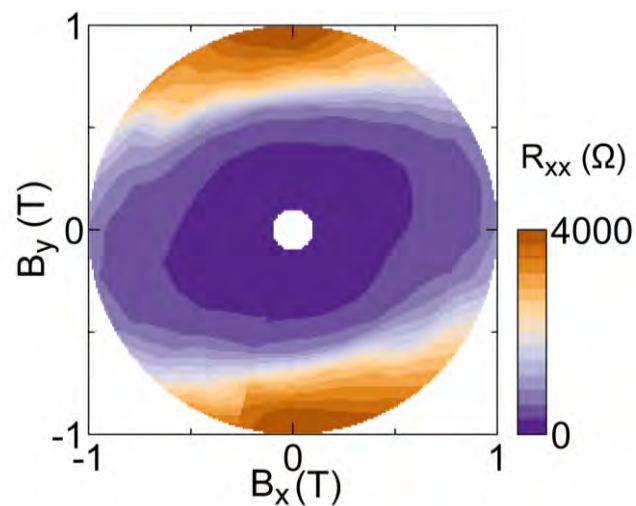
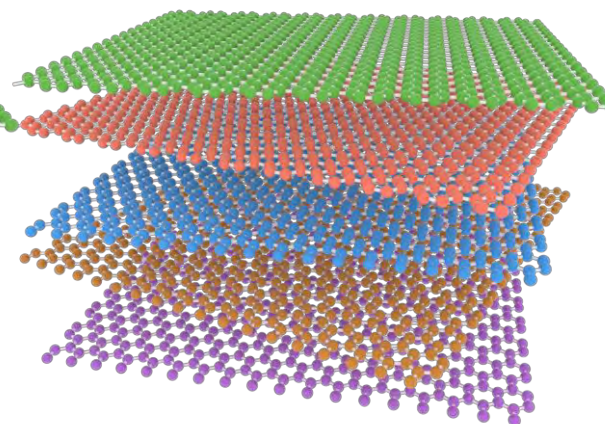
3L



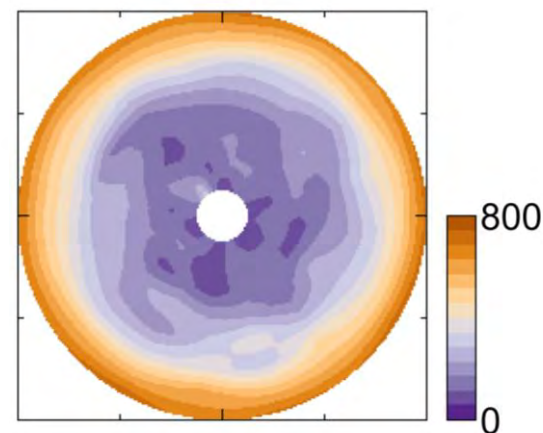
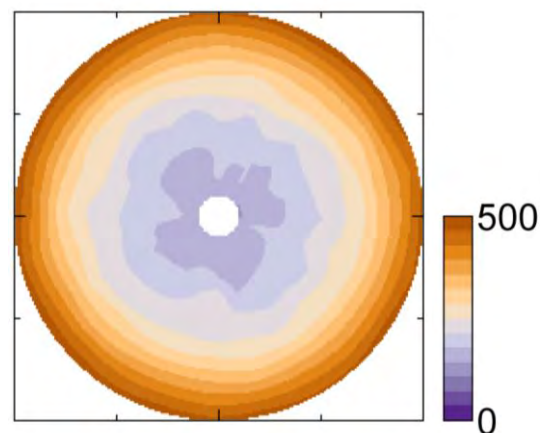
4L



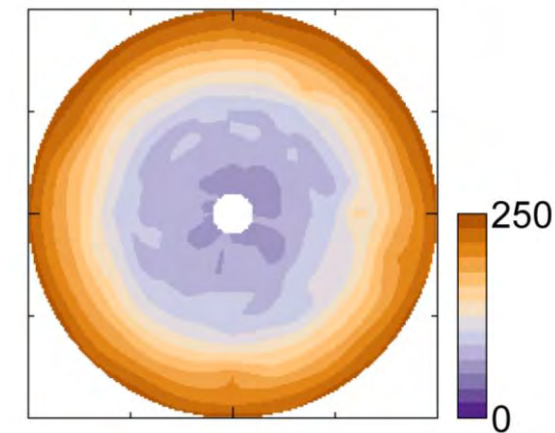
5L



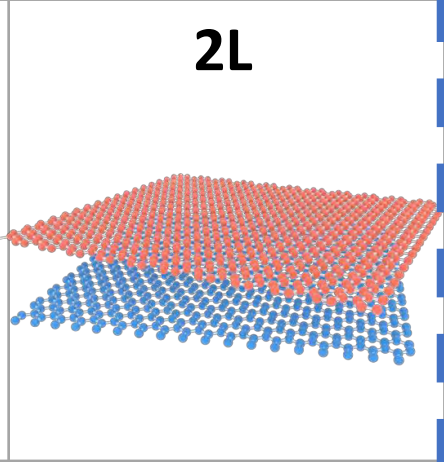
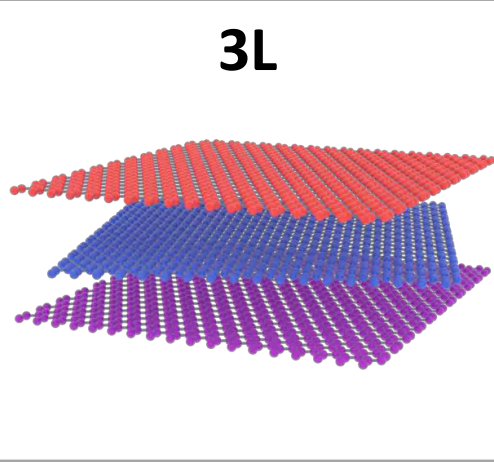
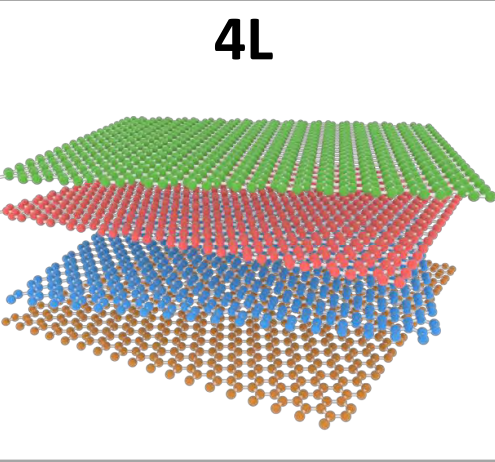
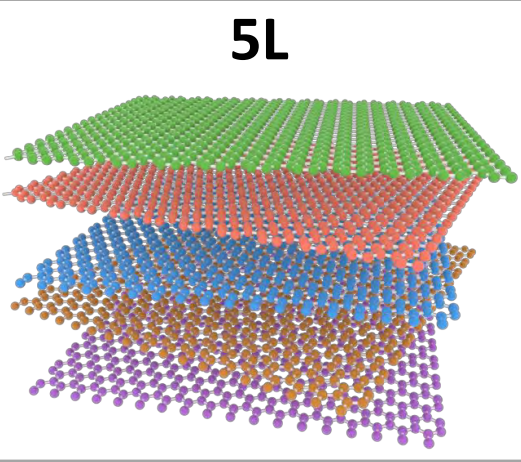
Anisotropic



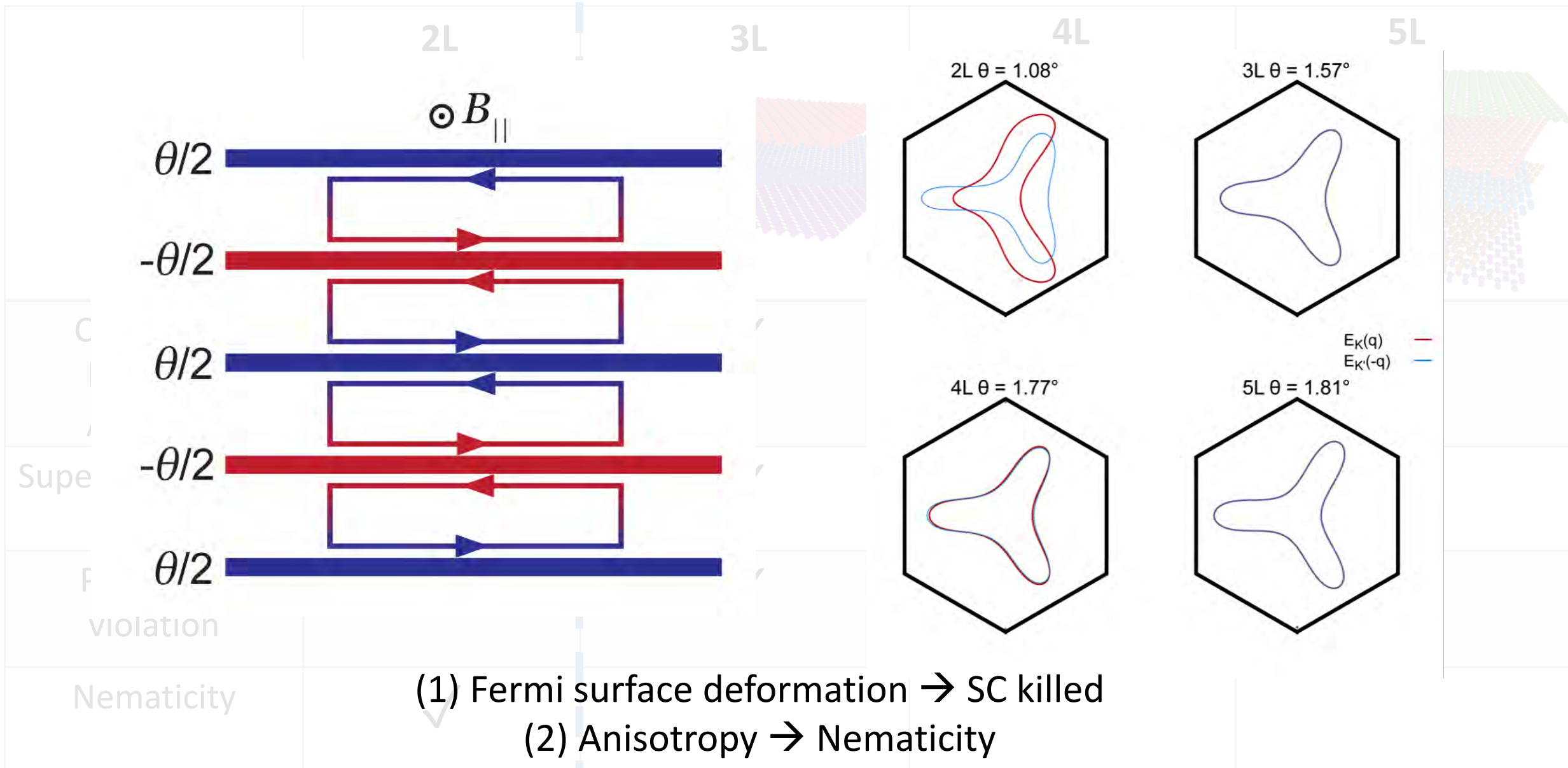
Isotropic



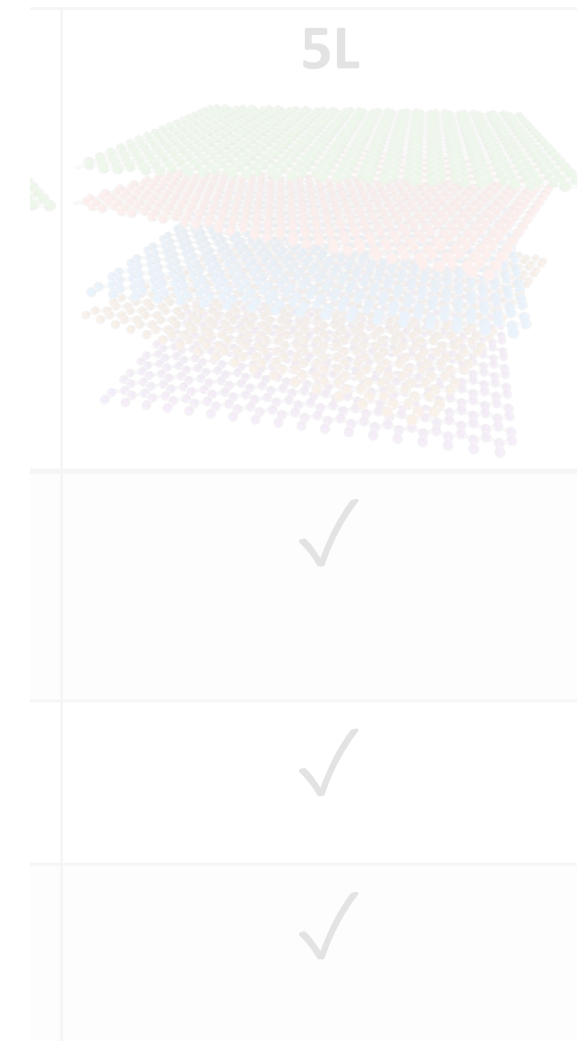
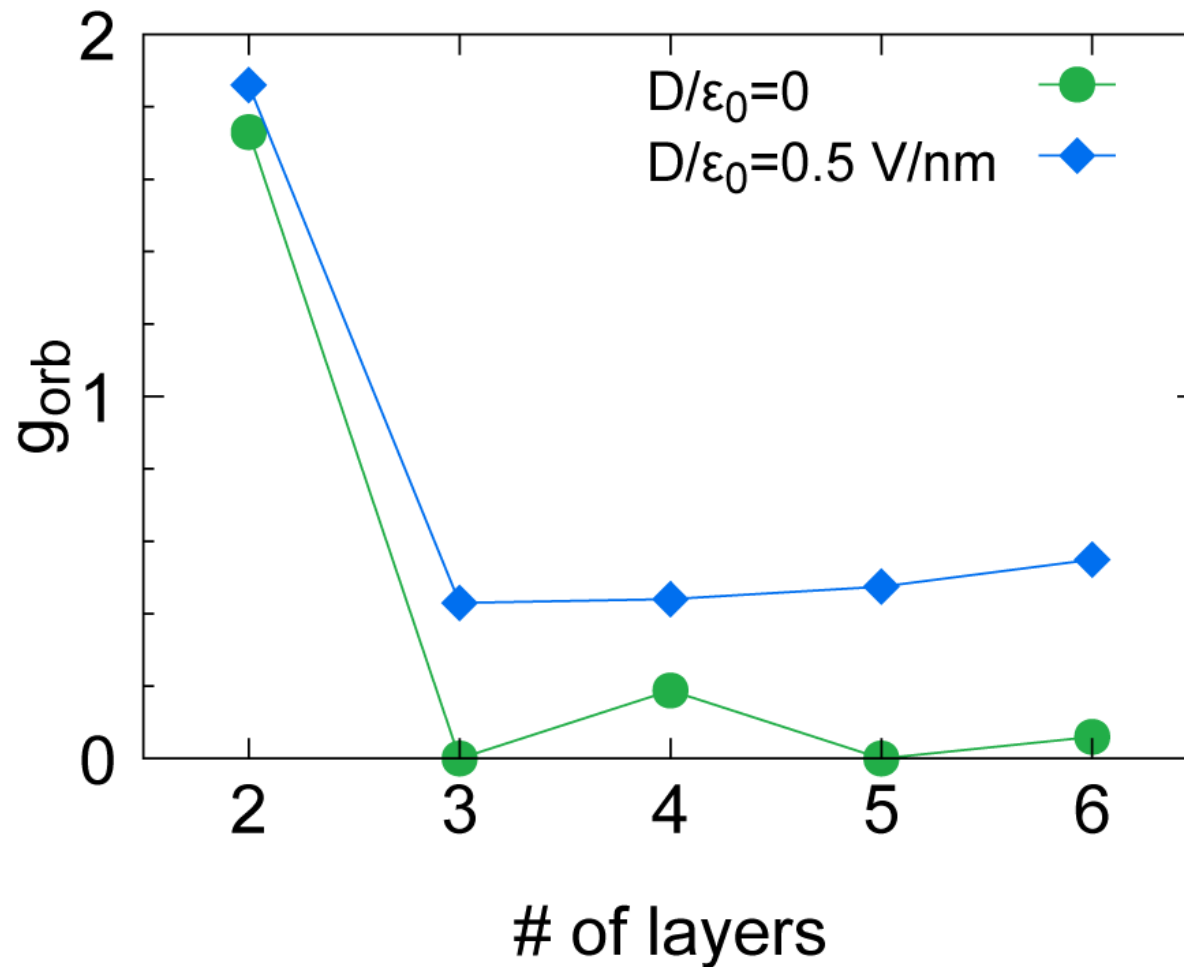
The magic family

	2L	3L	4L	5L
				
Correlated Insulator	✓	✓	✓	✓
Superconductivity	✓	✓	✓	✓
Pauli limit violation		✓	✓	✓
Nematicity	✓			

In-plane orbital effect



In-plane orbital effect



In-plane orbital effect explains the difference among the magic family members

✓ Can we design a tunable, strongly coupled superconductor?

Yes, much beyond! MATTG as a new platform for correlated physics

- Exceptional tunability for a new dimension in phase space
- Ultra-strongly coupled superconductivity
- Large Pauli limit violation and reentrant superconductivity

✓ Can we find important ingredients or recipes?

Yes, the *Magic family* of robust moiré superconductors is established

- All share the same type of flat band
- Importance of C_2T symmetry

Future directions

- SC order parameter of the magic family members, microscopic structure?
- Can we increase the T_c ? Or design ideas for high T_c ?
- Coupling with topological phases

Acknowledgement



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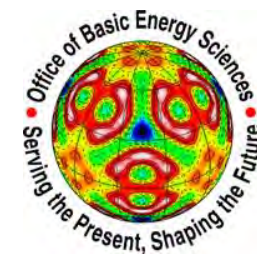


Yonglong Xie



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